



Генерация оптических гребенок на волоконных лазерах со встроенными оптическими микрорезонаторами

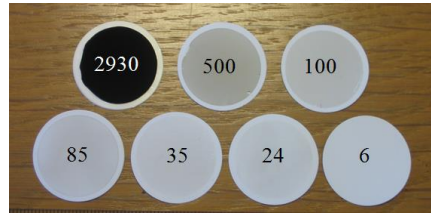
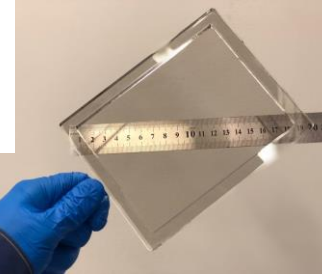
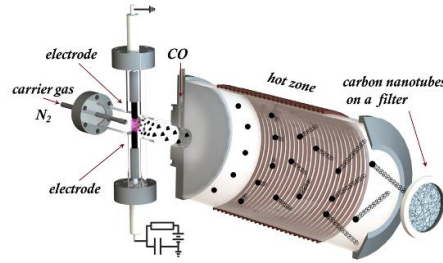
Юрий Гладуш

*Лаборатория Наноматериалов
Сколтех*

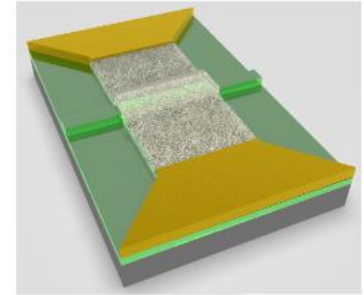
Laboratory of Nanomaterials



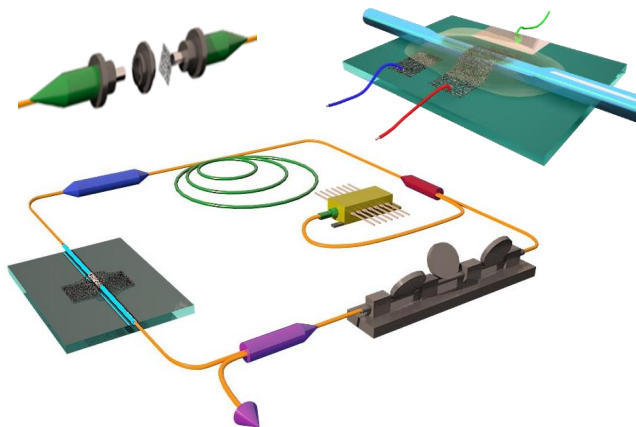
Carbon nanotubes



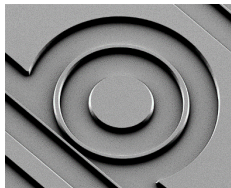
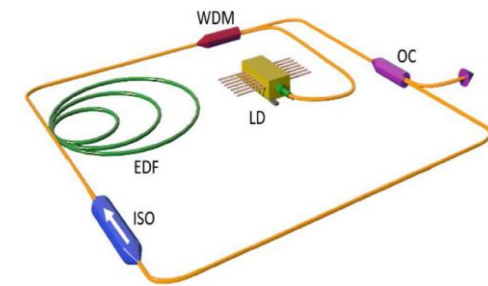
Integrated optical devices: wavelength converters, photodetectors



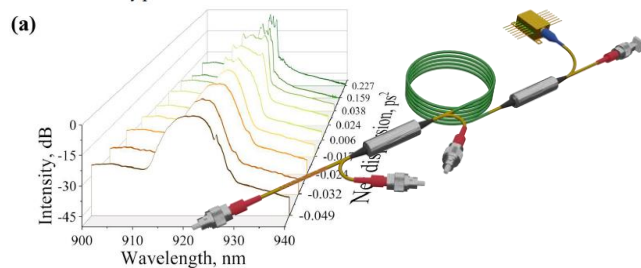
Ultrafast fiber lasers



Fiber lasers with integrated high-Q microcavity

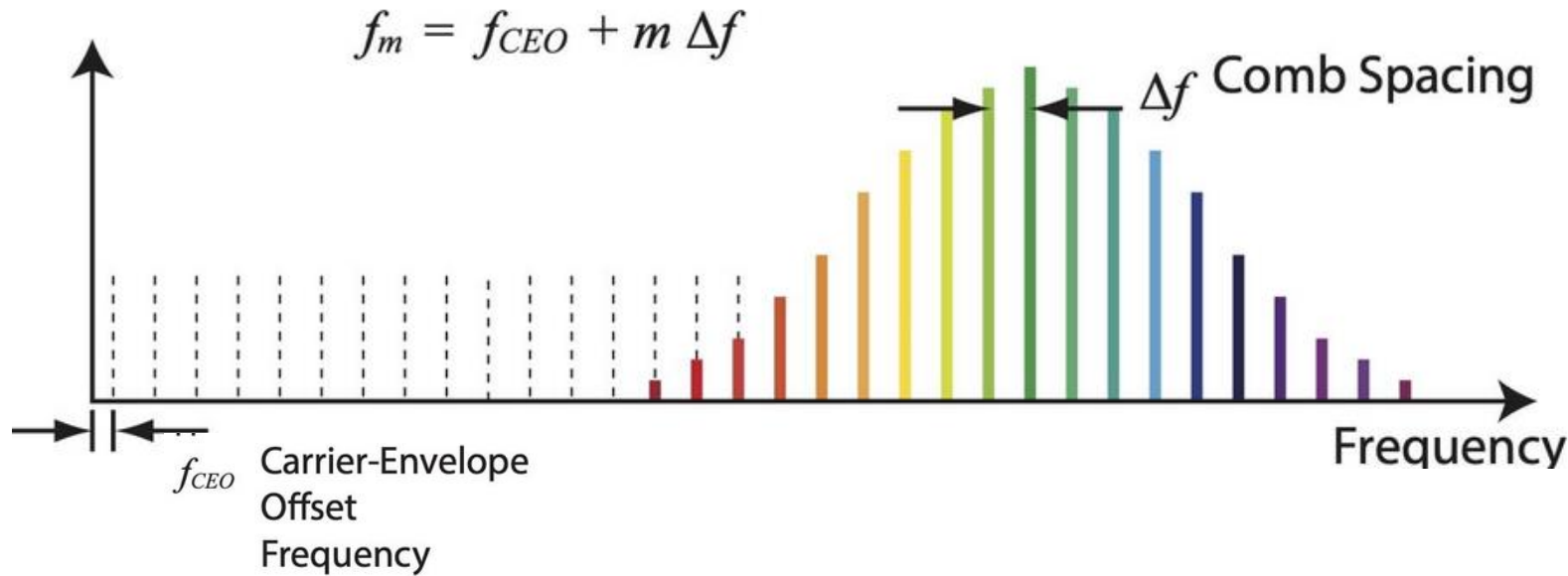


All-fiber femtosecond lasers at 920 nm

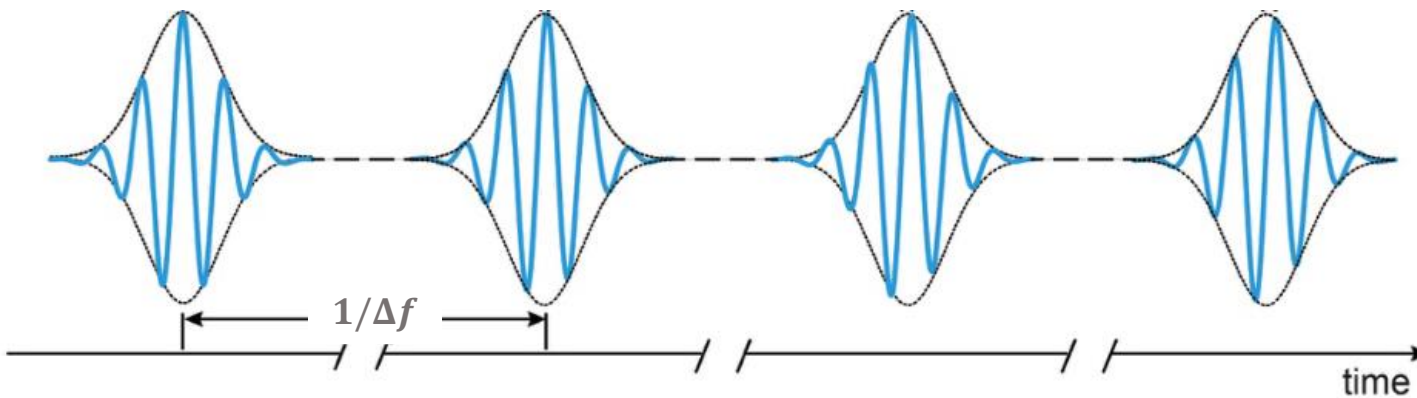


Optical frequency combs

Frequency domain



Time domain

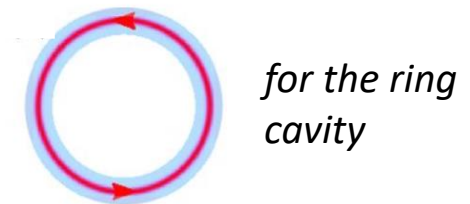


Comb characteristics:

$\Delta f \equiv$ Free Spectral Range (FSR)

Repetition rate:

$$T_R = \frac{1}{\Delta f} = \frac{L n_{gr}}{c}$$



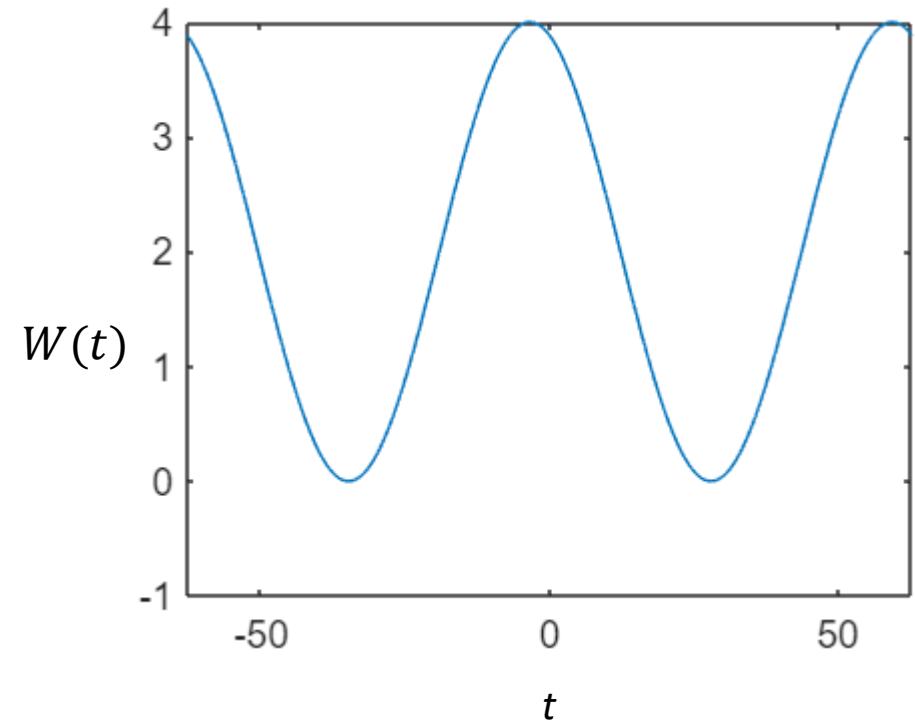
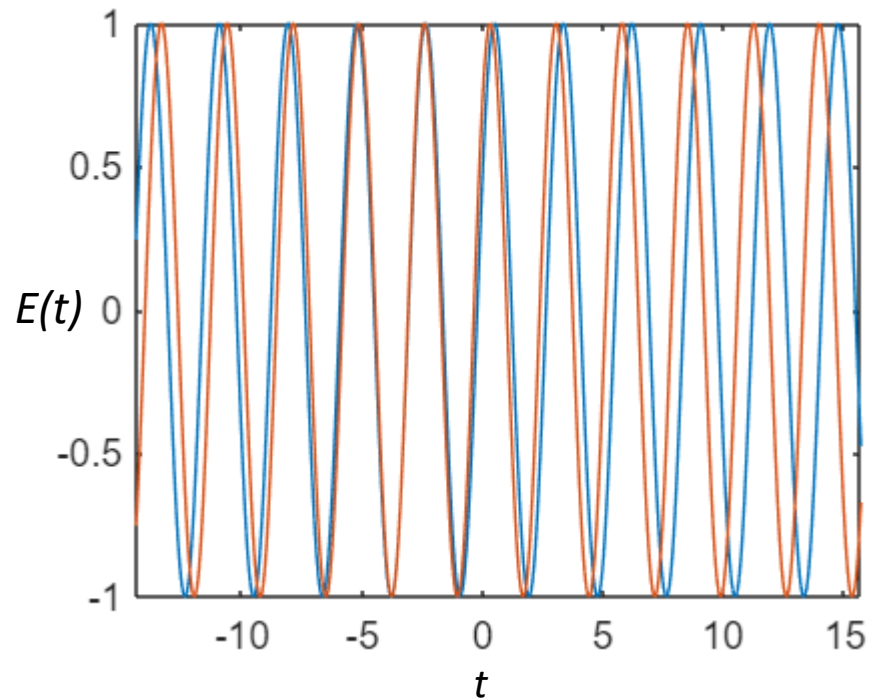
Comb width

Coherence

Examples of mode summation

2 modes

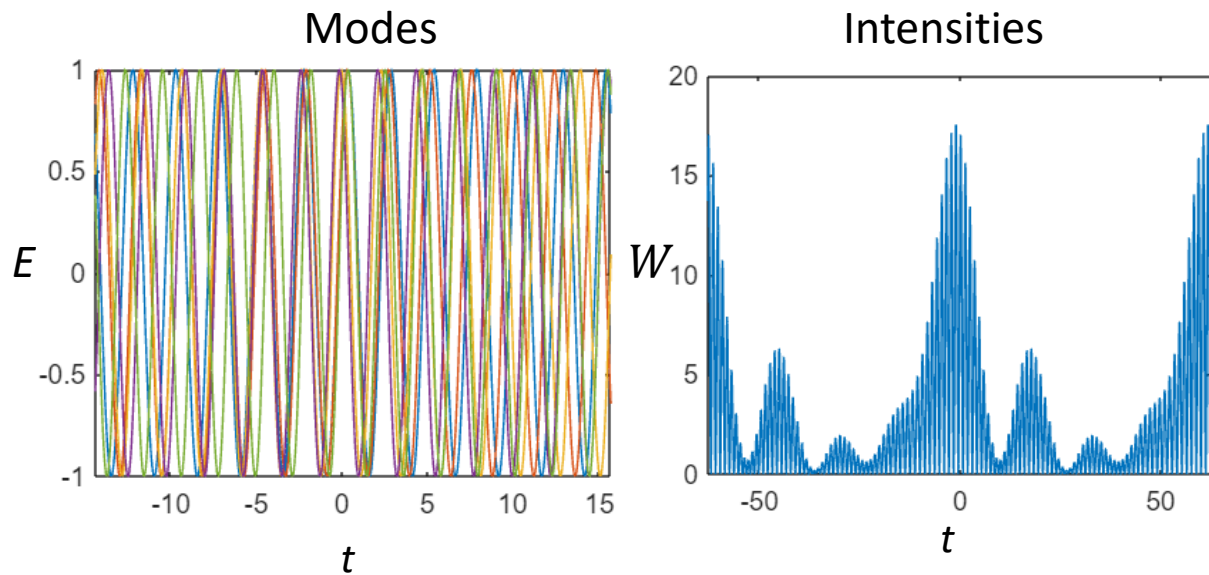
$$W(t) = \left| \sum_{l=0}^1 E_0 e^{i(\omega_0 + l\Delta\omega)t + i\varphi_l} \right|^2$$



Examples of mode summation

5 modes, random phase

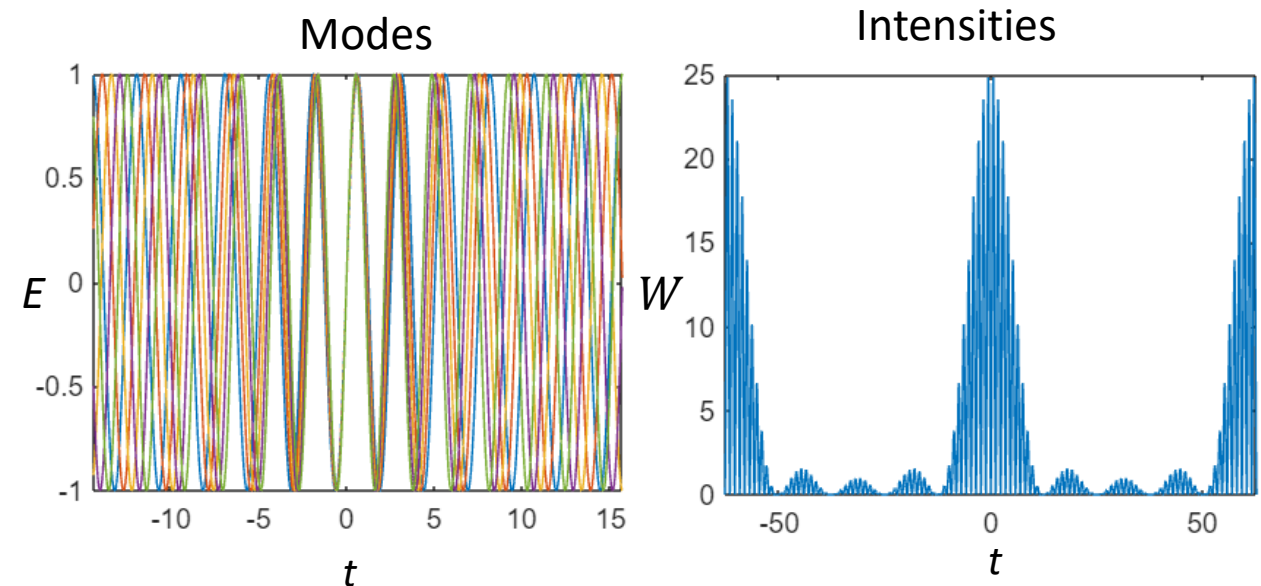
$$W(t) = \left| \sum_{l=0}^2 E_0 e^{i(\omega_0 + l\Delta\omega)t + i\varphi_l} \right|^2$$



5 modes, phase locked

$$W(t) = \left| \sum_{l=0}^2 E_0 e^{i(\omega_0 + l\Delta\omega)t + il\varphi_0} \right|^2$$

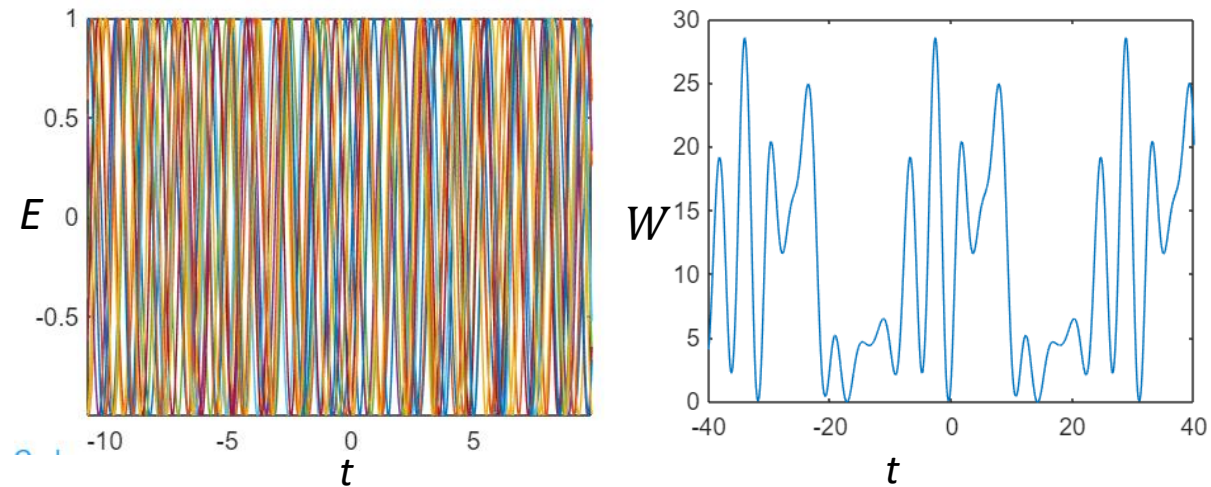
$$\varphi_{l+1} - \varphi_l = \varphi_0$$



Examples of mode summation

20 modes, random phase

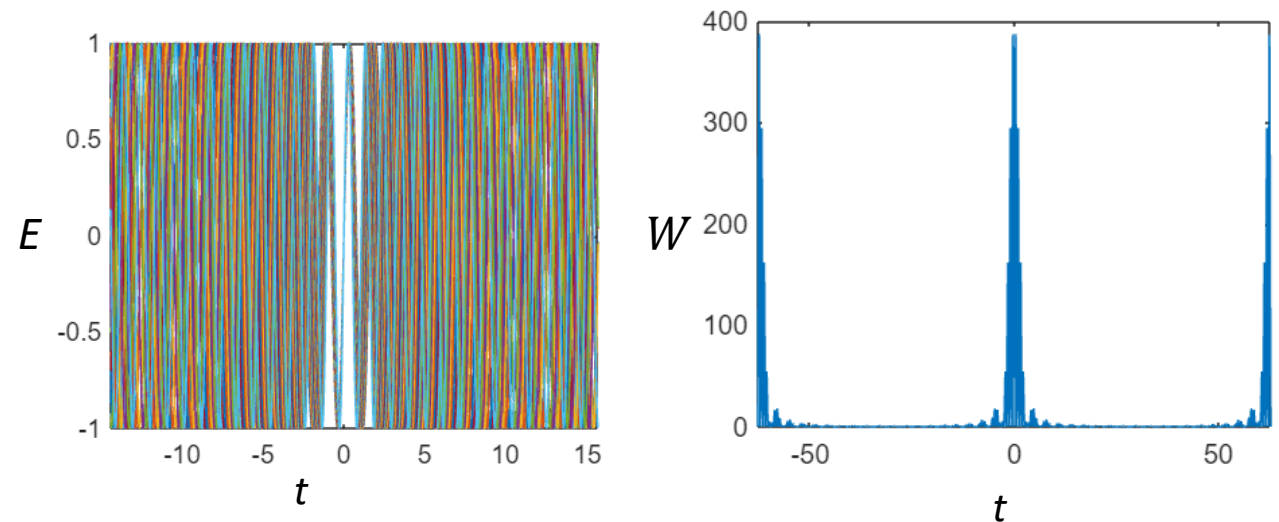
$$W(t) = \left| \sum_{l=0}^{19} E_0 e^{i(\omega_0 + l\Delta\omega)t + i\varphi_l} \right|^2$$



20 modes, phase locked

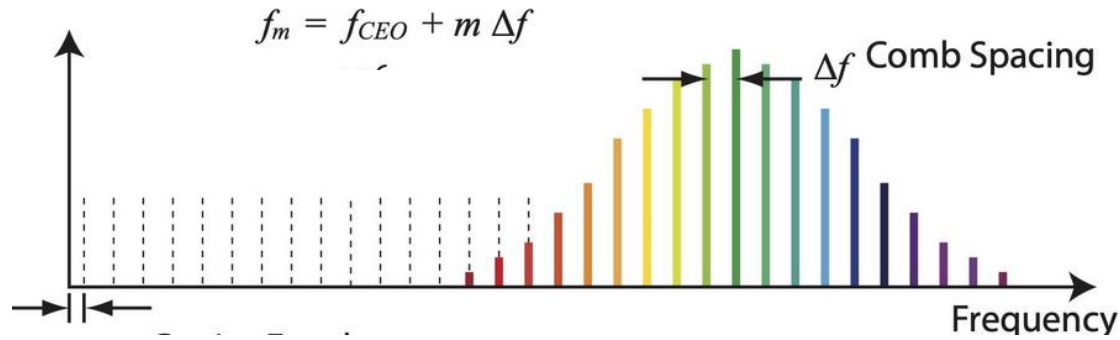
$$W(t) = \left| \sum_{l=0}^{19} E_0 e^{i(\omega_0 + l\Delta\omega)t + il\varphi_0} \right|^2$$

$$\varphi_{l+1} - \varphi_l = \varphi_0$$

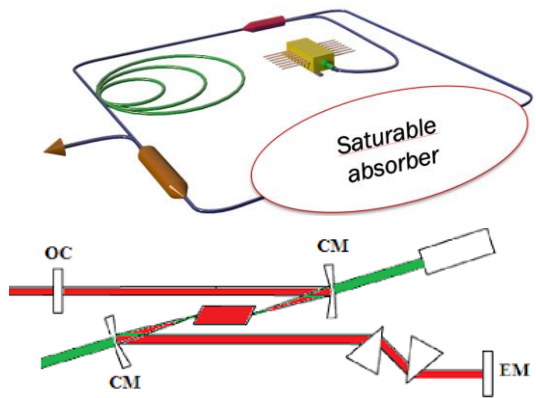


Optical frequency combs

Frequency domain

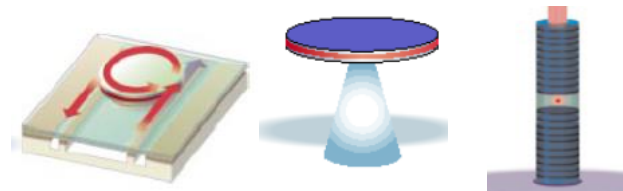


Mode-locked lasers



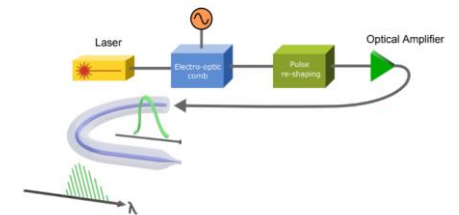
FSR=10 to 100 MHz

High-Q microcavities

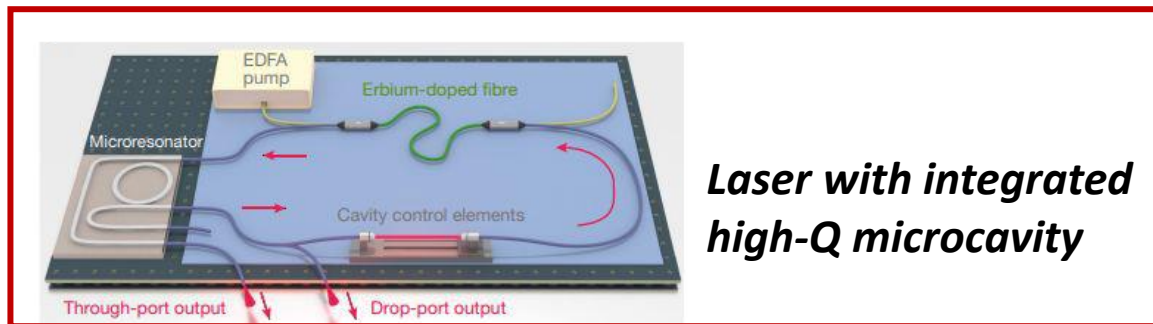


FSR=10 to 1000 GHz

Electro-optic comb generators

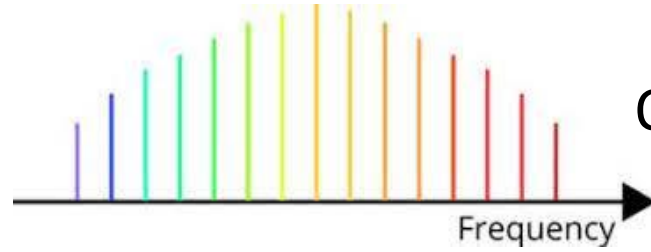


FSR up to 50 GHz

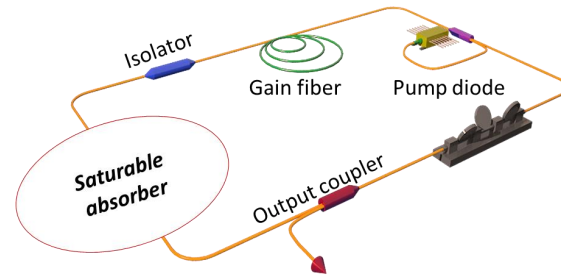


Laser with integrated high-Q microcavity

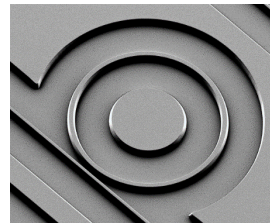
Content



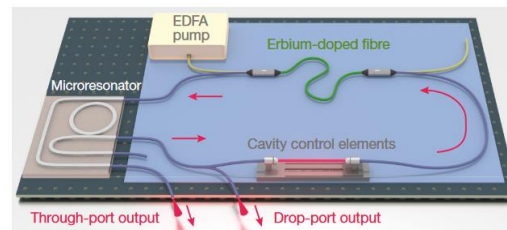
Optical frequency combs



Ultrafast fiber lasers

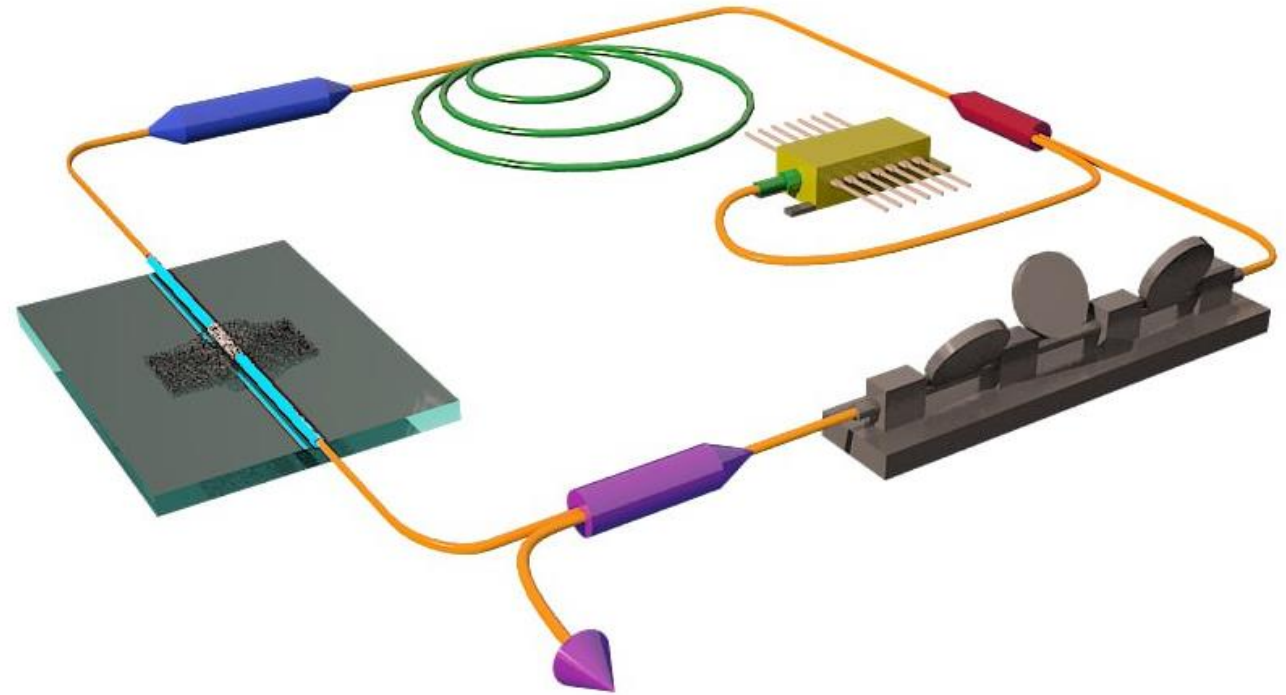


Microcavity combs



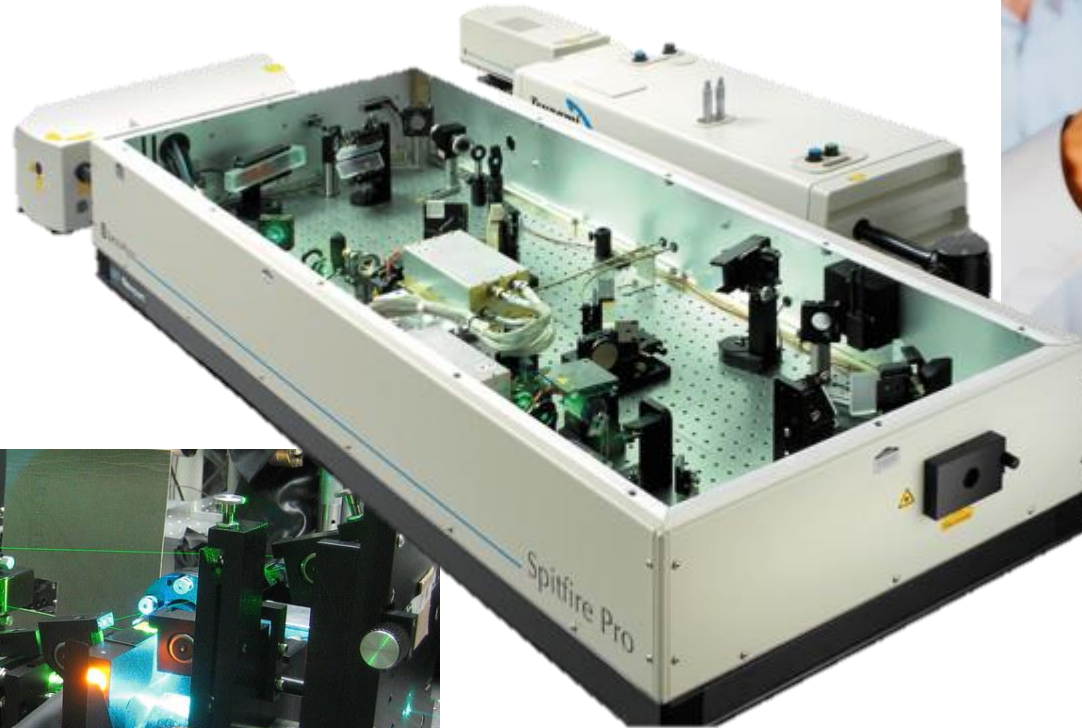
Laser microcavity combs

Ultrafast fiber lasers



Mode-locked femtosecond lasers

Ti:Sa lasers (1980x)



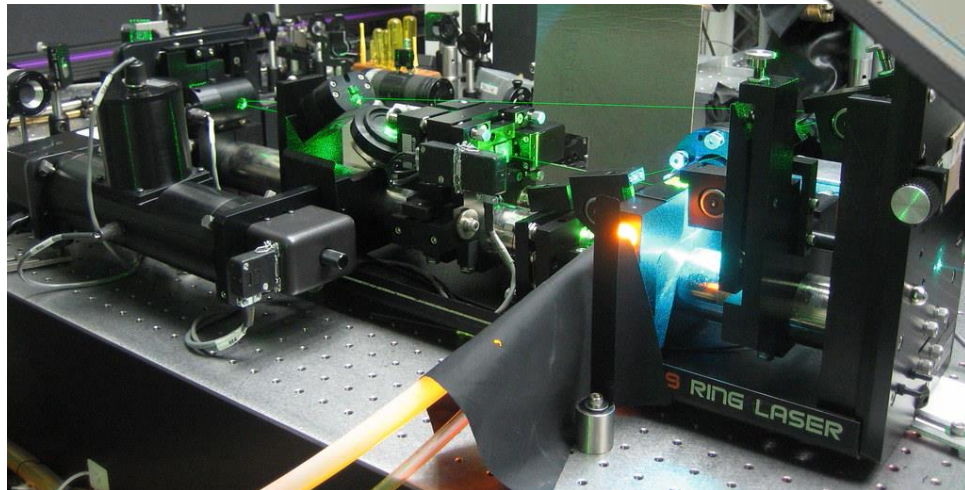
Fiber lasers



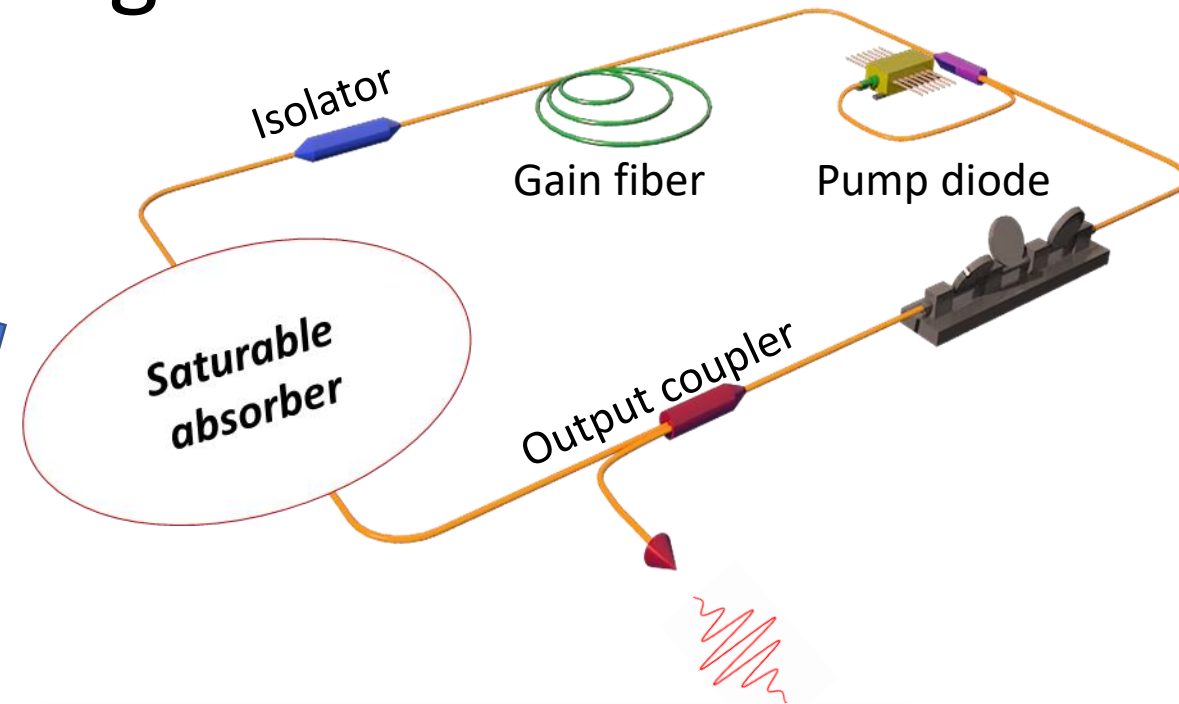
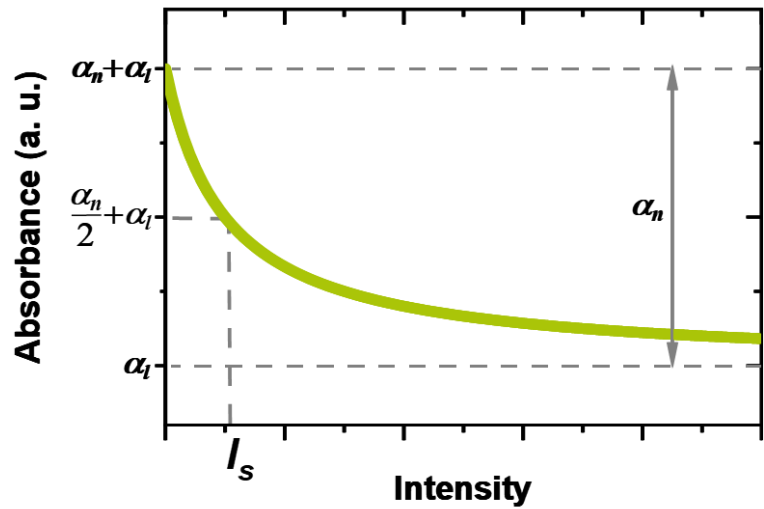
Semiconductor lasers



Dye lasers (1972)

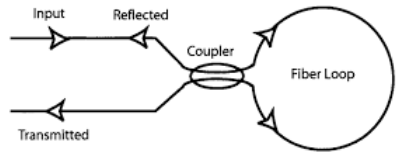
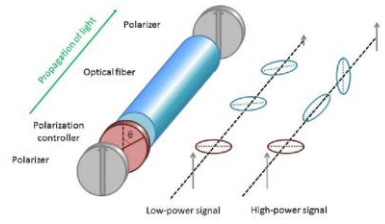
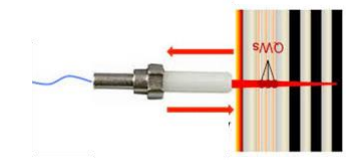


Fiber laser mode locking mechanism

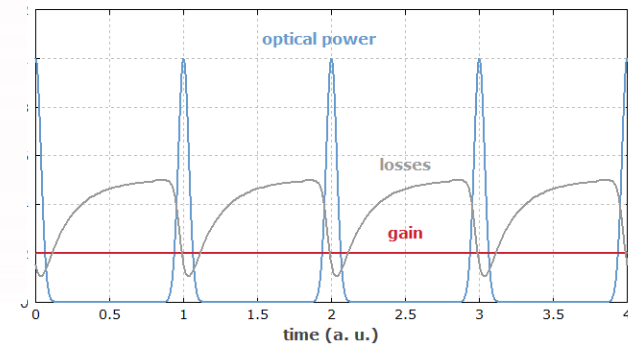
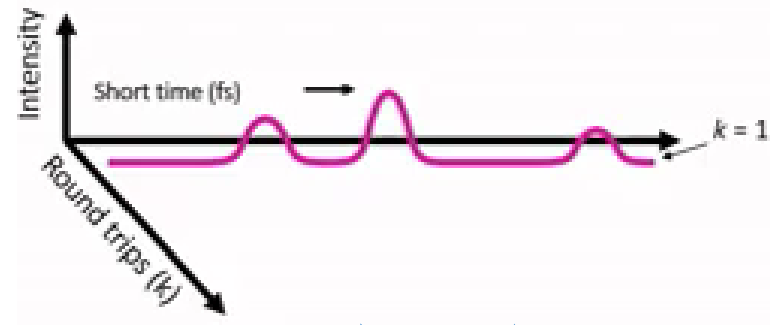


Material SA

Artificial SA



Schematic of an all-fiber Sagnac interferometer acting as a nonlinear optical loop mirror whose transmission depends on launched input power.



Weak pulses suppressed, strong pulse shortens and amplified

Fiber mode locked lasers

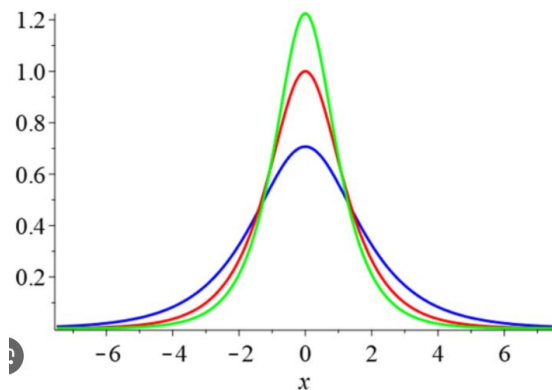
$$\underbrace{\frac{\partial E(z, T)}{\partial z} - \frac{1}{v_g} \frac{\partial E(z, T)}{\partial t}}_{\text{Pulse propagation}} = \underbrace{[g + D_g \frac{\partial^2}{\partial t^2}]}_{\text{gain + spectral filter}} - \underbrace{l_0}_{\text{losses}} - \underbrace{\frac{\kappa}{1 + |E|^2/I_{sat}}}_{\text{saturable absorber}} + \underbrace{iD_2 \frac{\partial^2}{\partial t^2}}_{\text{Dispersion}} - \underbrace{i\gamma_K |E|^2}_{\text{Nonlinearity}} E(z, T)$$

Soliton solution (anomalous dispersion):

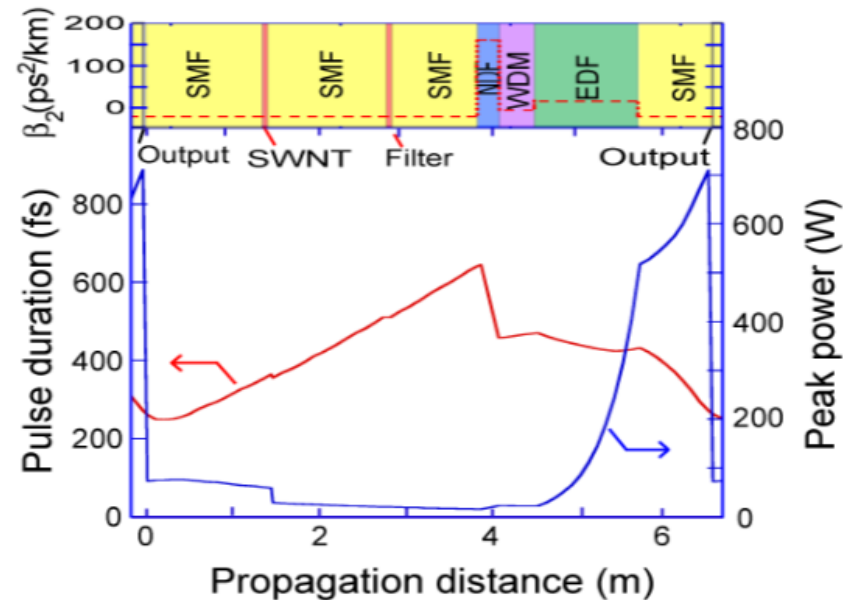
$$E = \eta \operatorname{sech}((t-z/v_g)/\tau_p) e^{i\eta^2 z/L_D}$$

Soliton area theorem:

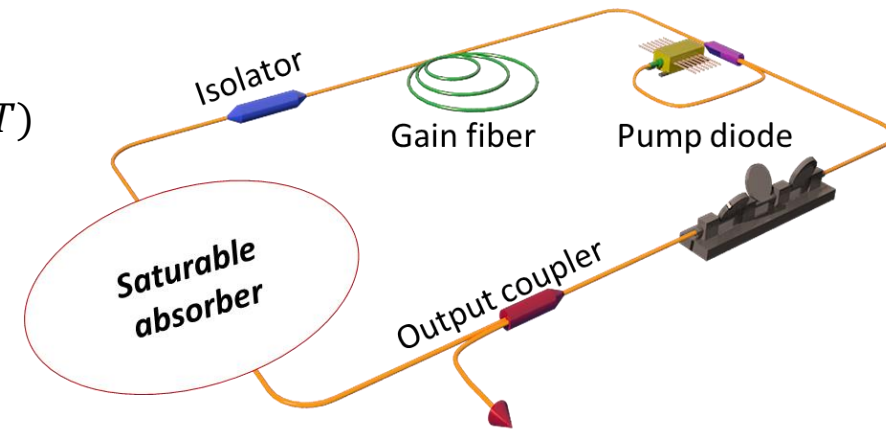
$$W_{pulse} = \frac{|D_2|}{\gamma_K \tau_p} = \frac{3.11 |D_2|}{\gamma_K \tau_{FWHM}}$$



In **real laser** soliton parameters are constantly changing

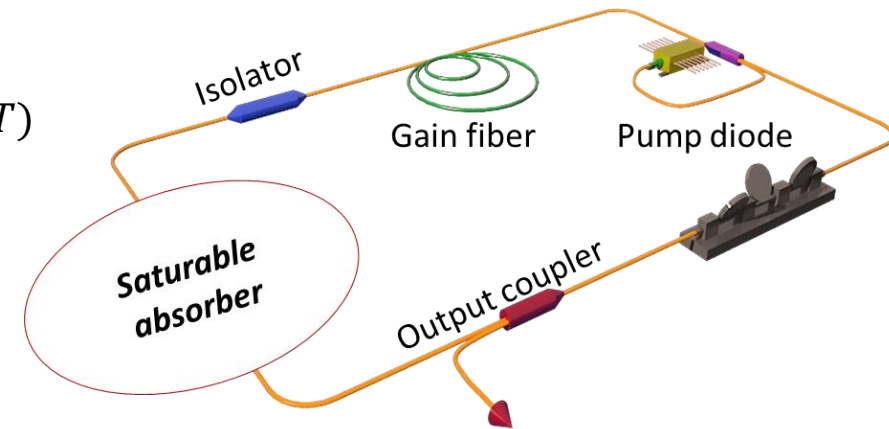


N. Nishizawa et al, Photonics 2(3):808-824, 2015

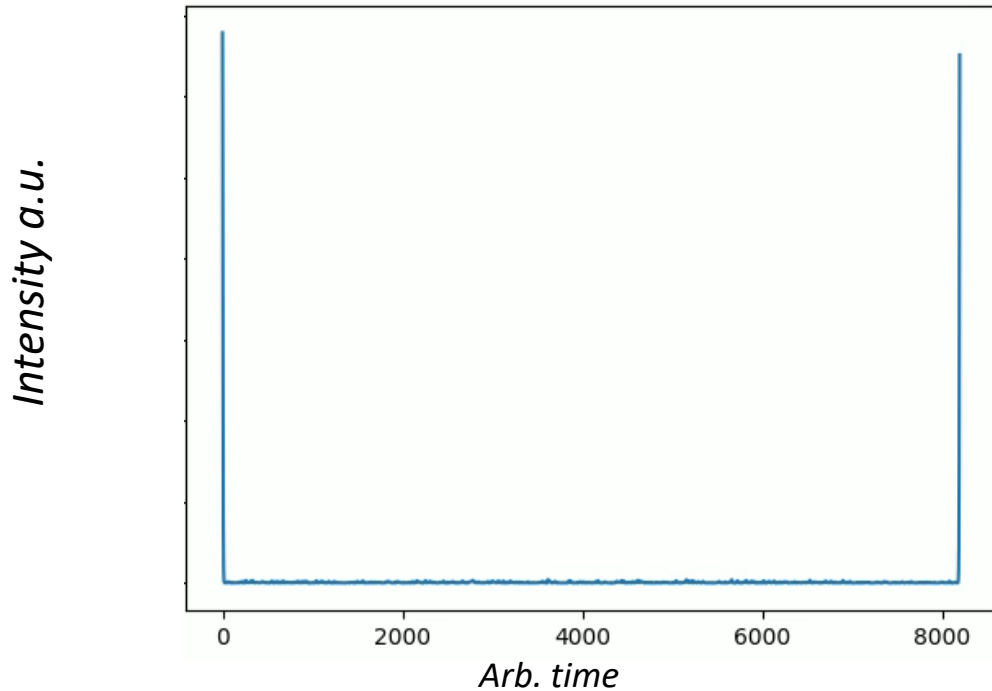


Fiber mode locked lasers

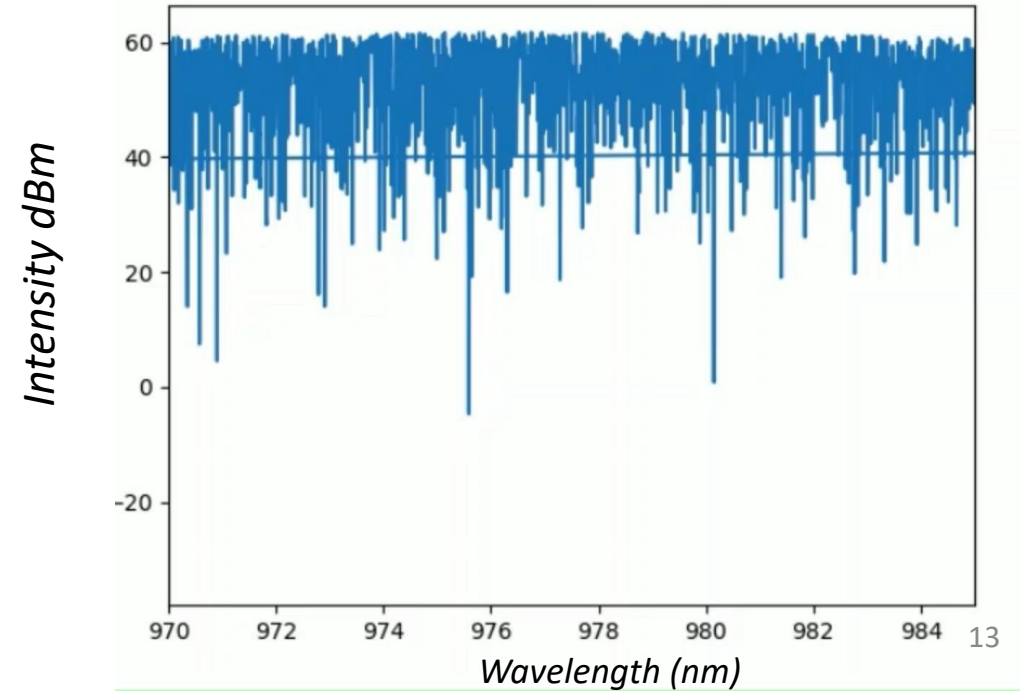
$$\underbrace{\frac{\partial E(z, T)}{\partial z} - \frac{1}{v_g} \frac{\partial E(z, T)}{\partial t}}_{\text{Pulse propagation}} = \underbrace{[g + D_g \frac{\partial^2}{\partial t^2}]}_{\text{gain + spectral filter}} - \underbrace{l_0}_{\text{losses}} - \underbrace{\frac{\kappa}{1 + |E|^2/I_{sat}}}_{\text{saturable absorber}} + \underbrace{iD_2 \frac{\partial^2}{\partial t^2}}_{\text{Dispersion}} - \underbrace{i\gamma_K |E|^2}_{\text{Nonlinearity}} E(z, T)$$



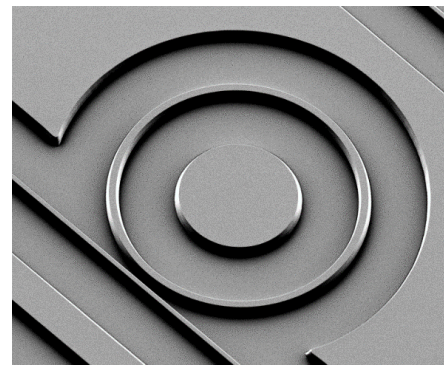
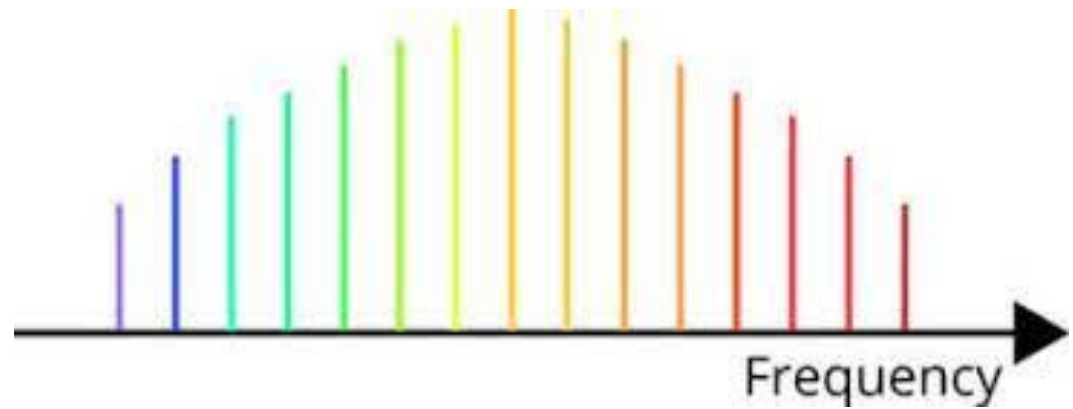
Numerical simulation (time domain)



Numerical simulation (spectrum)

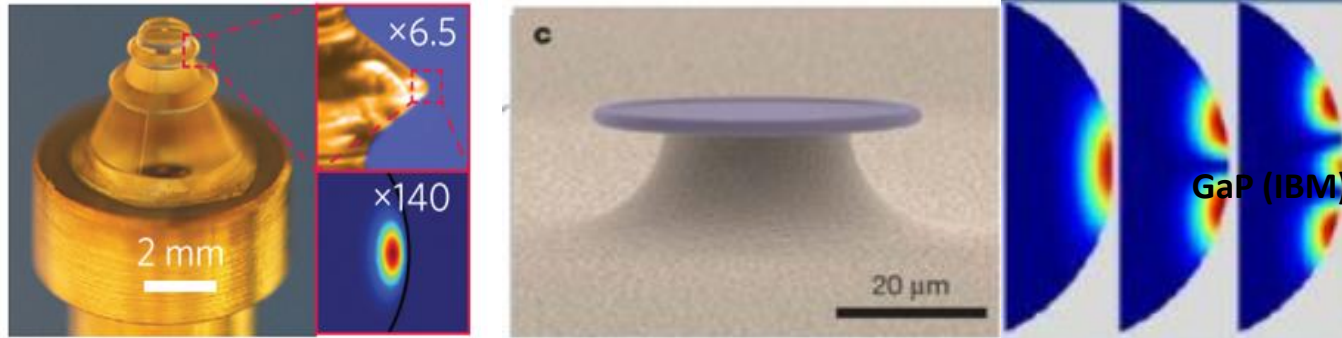


Microcavity frequency combs

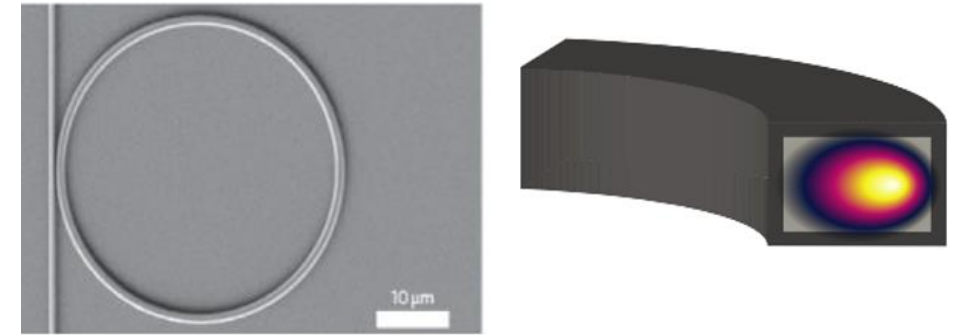


Platforms for soliton microcomb generation

Whispering gallery mode cavities

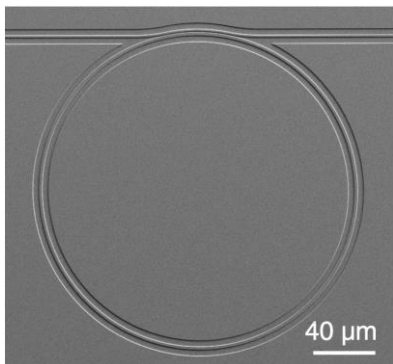


Integrated microrings

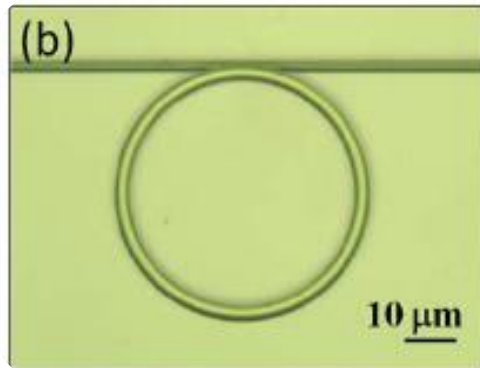


Microring platforms

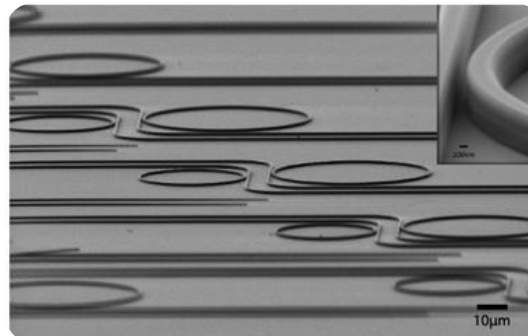
LiNbO₃
(Rochester, Caltech)



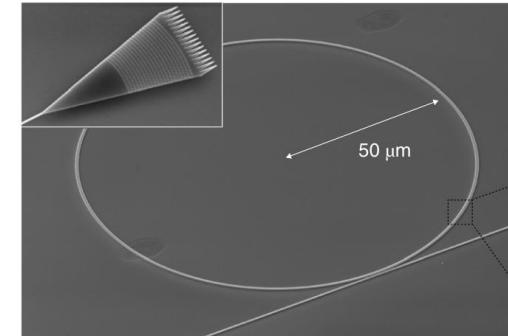
AlN (Yale),
AlGaAs (NIST)



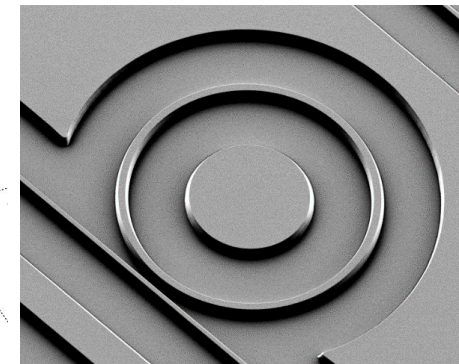
Diamond (Harvard)



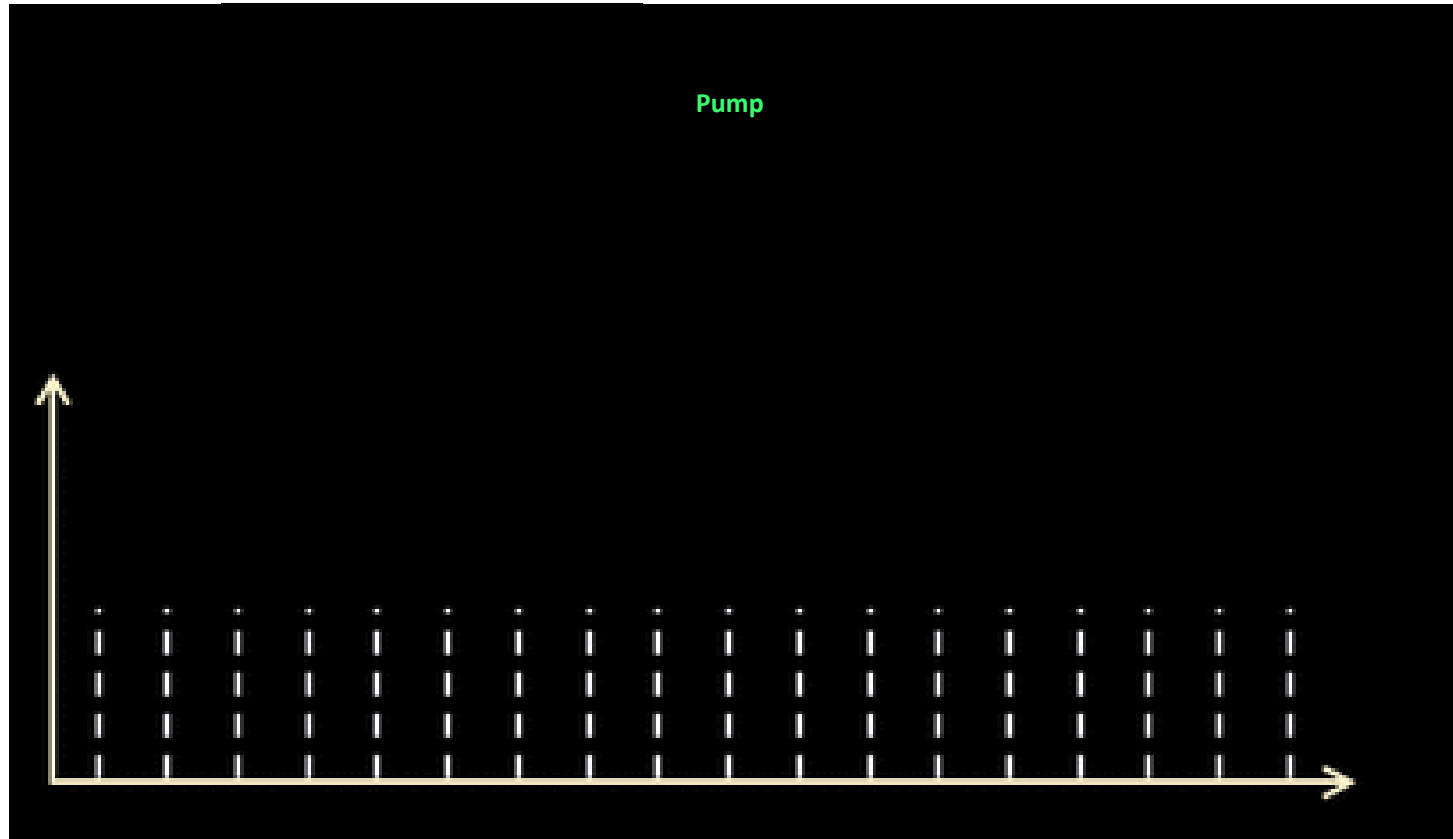
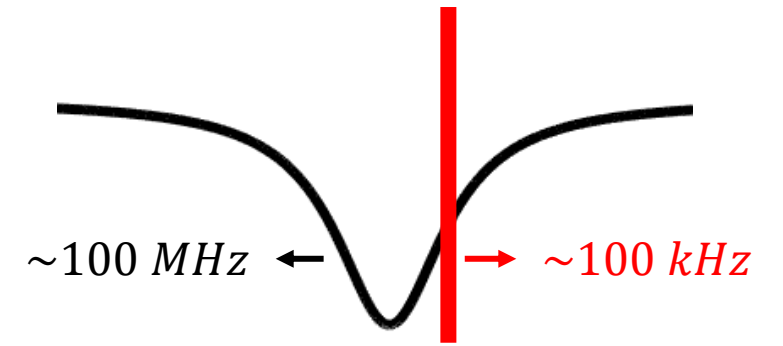
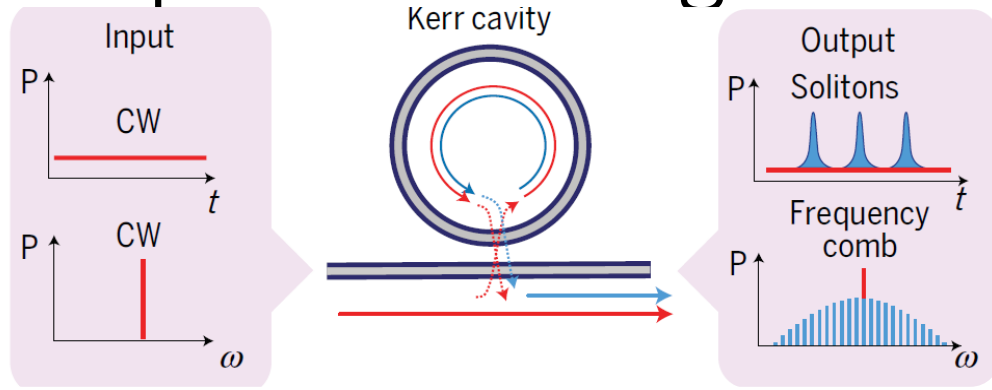
GaP (IBM)



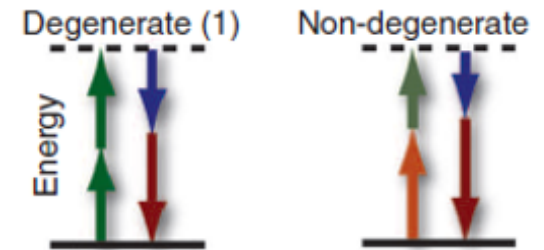
Silicon Nitride
(Columbia, UCSB, EPFL)



Principle of comb generation



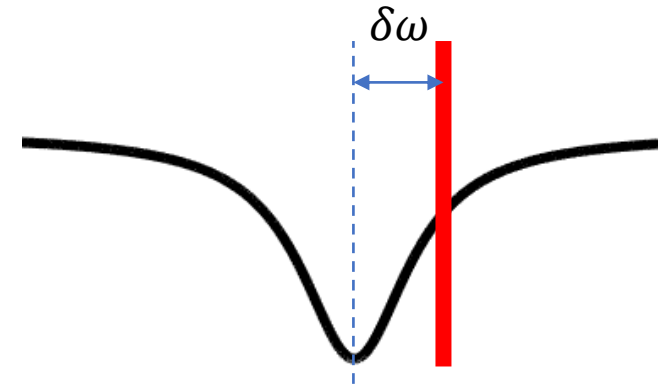
Energy is transferred from initial mode to neighboring mode by four wave mixing mechanism



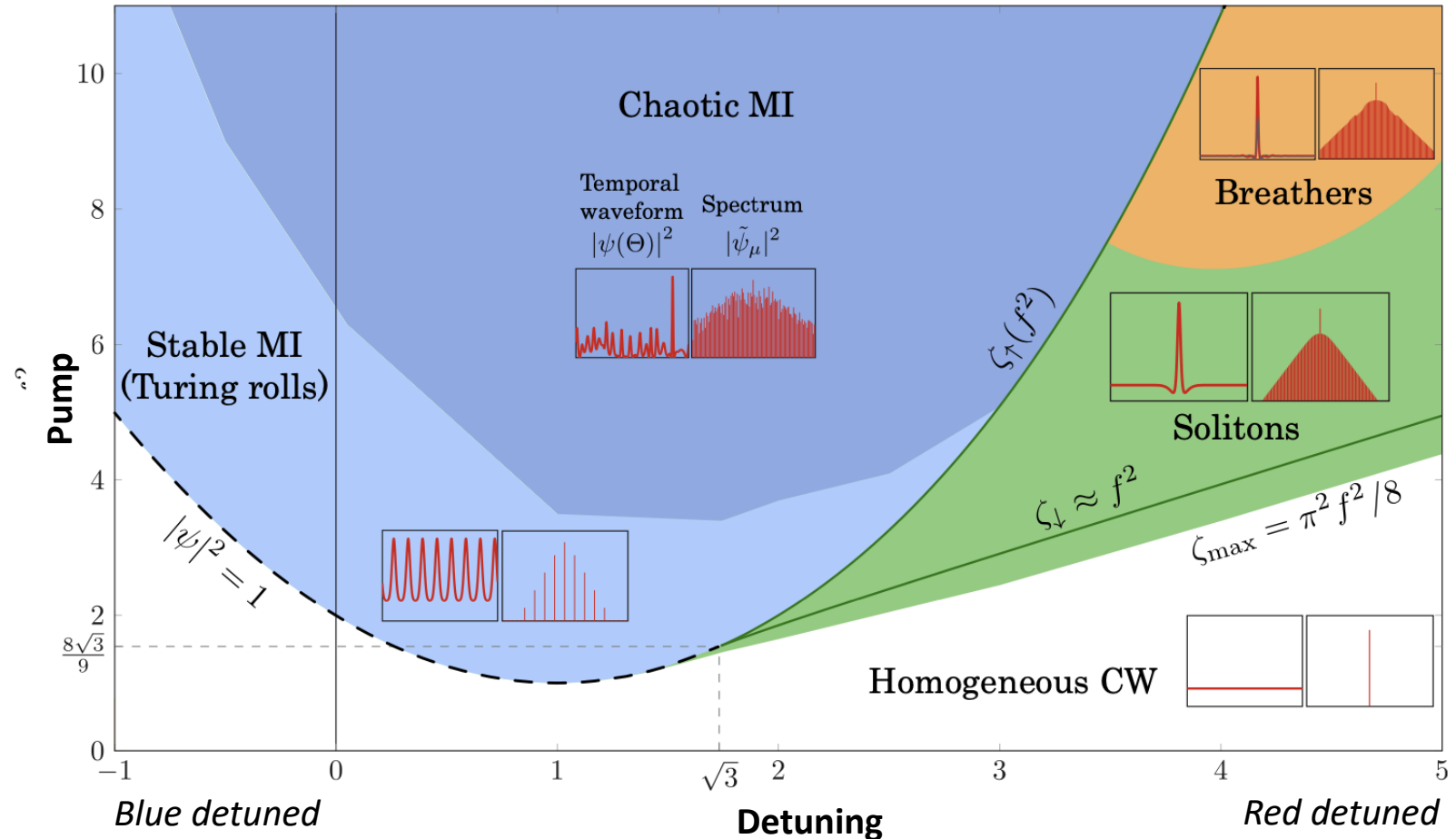
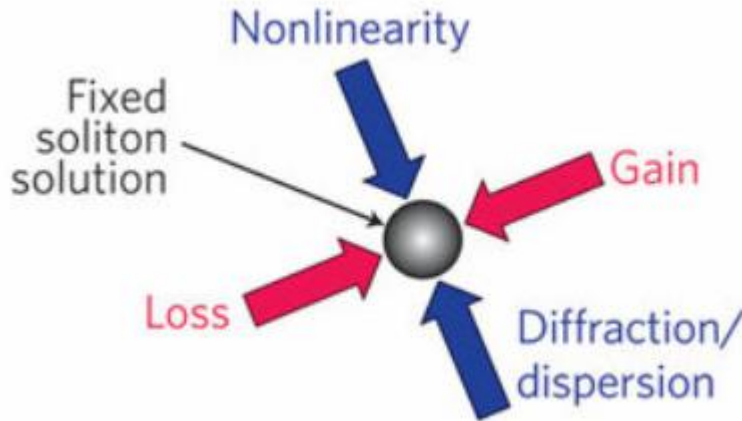
LLE equation

Lugiato-Lefever equation (LLE)

$$\frac{\partial A}{\partial t} = \left(\underbrace{-\left(\frac{\kappa}{2} + i\delta\omega\right)}_{\text{Loss Detuning}} + i \underbrace{\frac{D_2}{2} \frac{\partial^2}{\partial \phi^2}}_{\text{Dispersion}} + i \underbrace{g_0 |A|^2}_{\text{Nonlinearity}} \right) A + \underbrace{\sqrt{\kappa_{\text{ex}}} \sin}_{\text{Pump}}$$



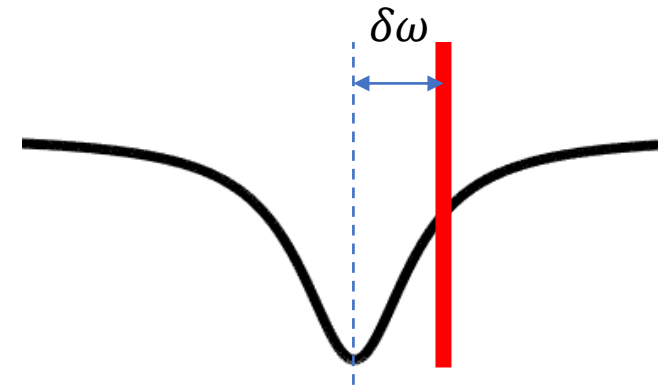
Temporal cavity soliton – a localized structure emerging as interplay of nonlinearity and dispersion on one side and losses and pump on the other.



LLE equation

Lugiato-Lefever equation (LLE)

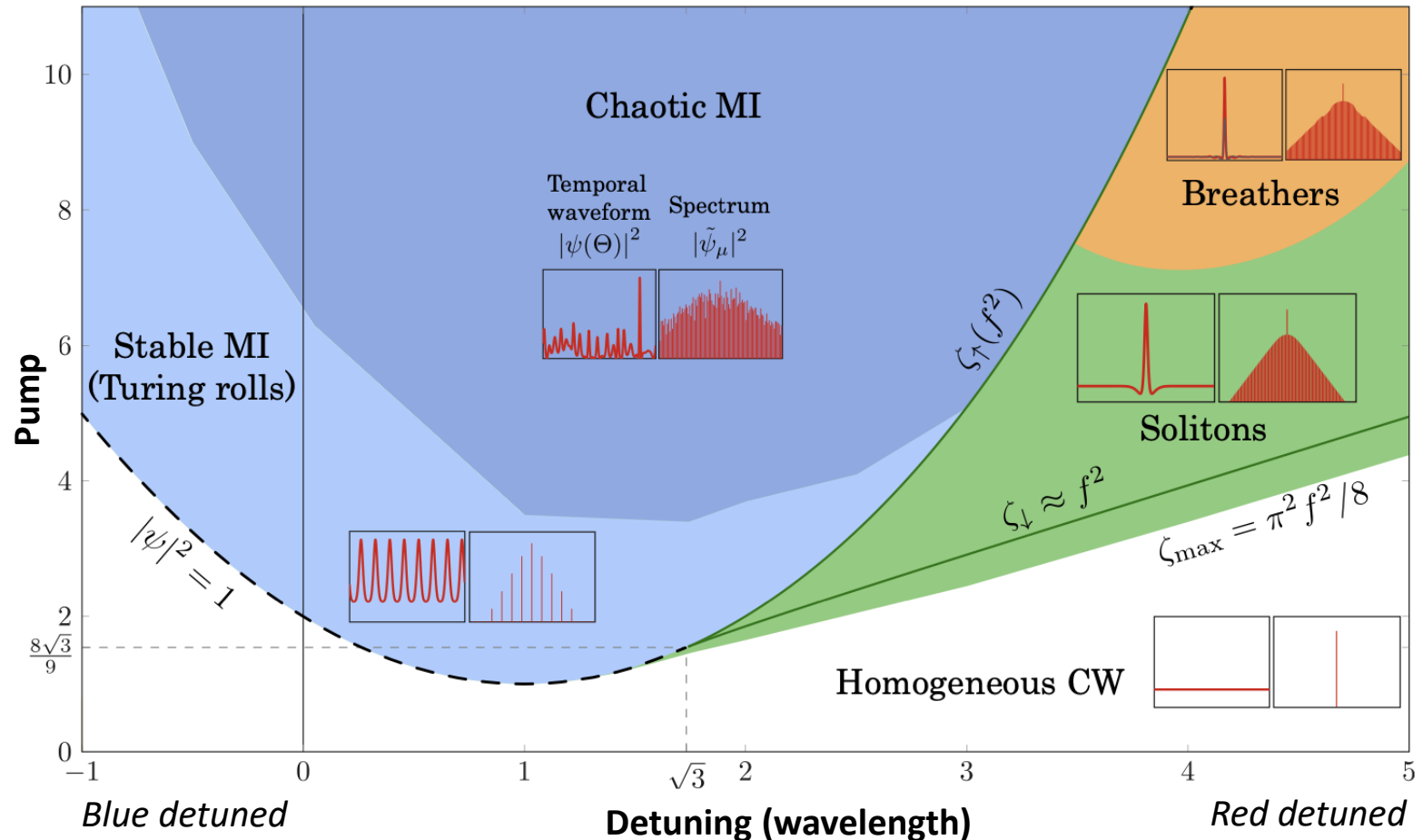
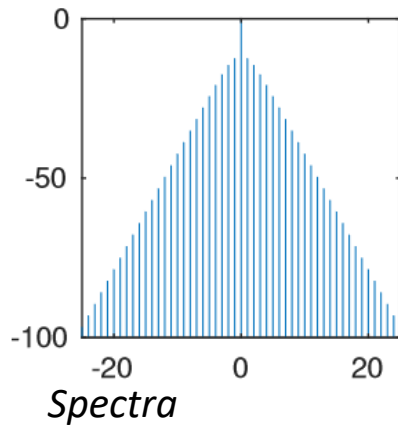
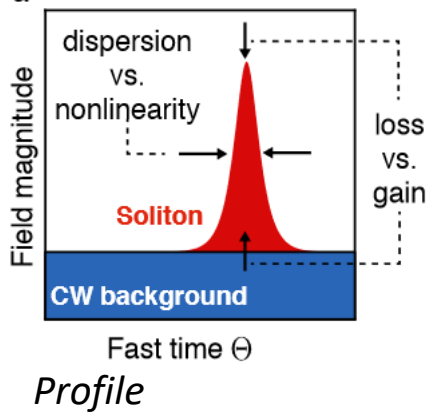
$$\frac{\partial A}{\partial t} = \left(\underbrace{-\left(\frac{\kappa}{2} + i\delta\omega\right)}_{\text{Loss Detuning}} + i \underbrace{\frac{D_2}{2} \frac{\partial^2}{\partial \phi^2}}_{\text{Dispersion}} + i \underbrace{g_0 |A|^2}_{\text{Nonlinearity}} \right) A + \underbrace{\sqrt{\kappa_{\text{ex}}} \sin}_{\text{Pump}}$$



Exact soliton solution is not known

Approximate solution of NLSE (cavity solitons):

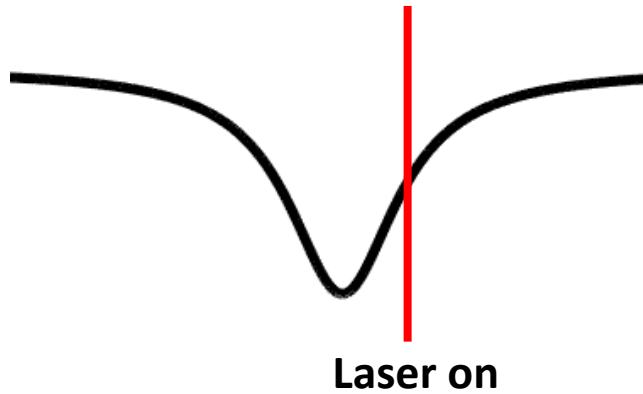
$$A(t, \tau) = \sqrt{\frac{2\delta\omega}{g_0}} \operatorname{sech}\left(\frac{\tau}{\Delta\tau_s}\right)$$



Real life

Lugiato-Lefever equation (LLE)

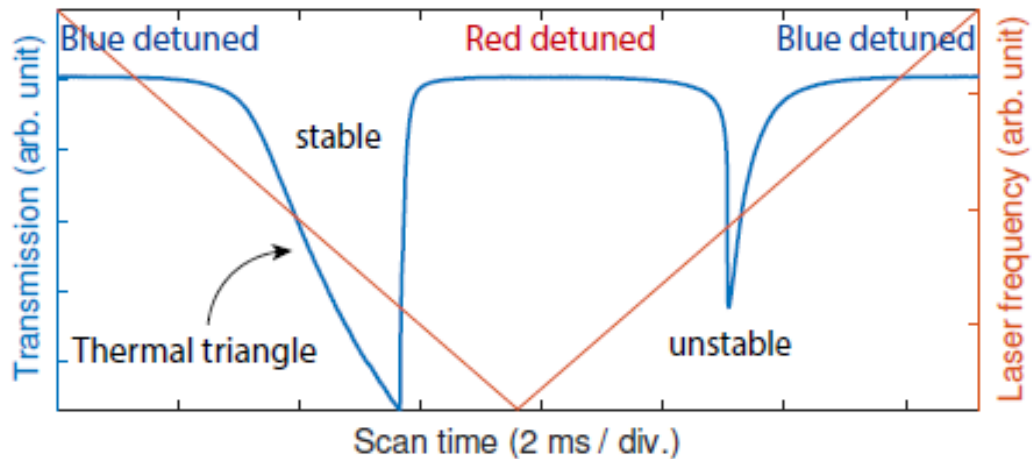
$$\frac{\partial A}{\partial t} = \left(\underbrace{-\left(\frac{\kappa}{2} + i\delta\omega\right)}_{\text{Loss Detuning}} + i \underbrace{\frac{D_2}{2} \frac{\partial^2}{\partial \phi^2}}_{\text{Dispersion}} + i \underbrace{g_0 |A|^2}_{\text{Nonlinearity}} \right) A + \underbrace{\sqrt{\kappa_{\text{ex}}} S_{\text{in}}}_{\text{Pump}}$$



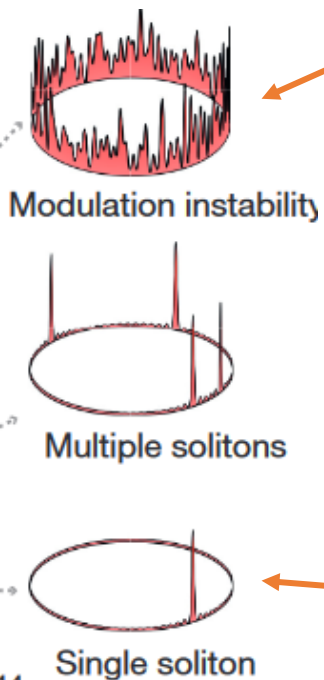
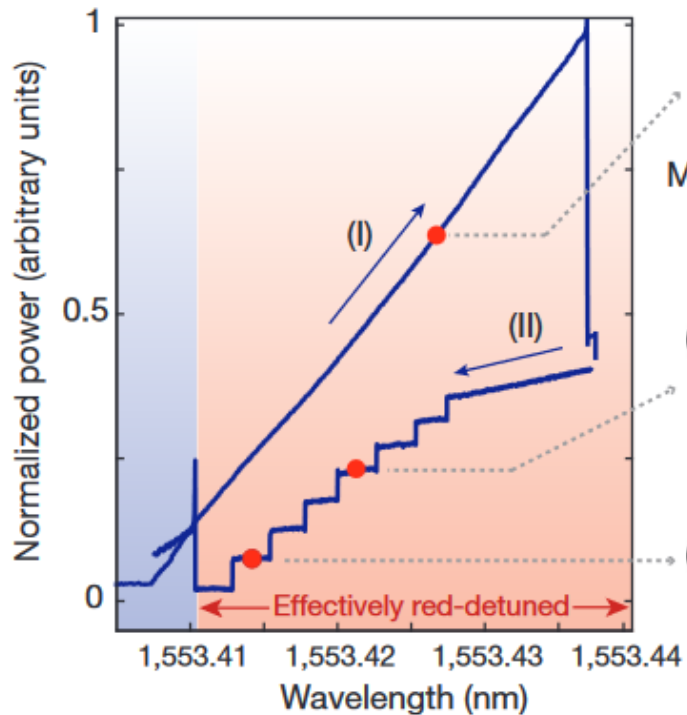
Once you tune the laser to the resonance, it shifts:

Instant shift due to self phase modulation
($n = n_0 + g_0 |A|^2$)

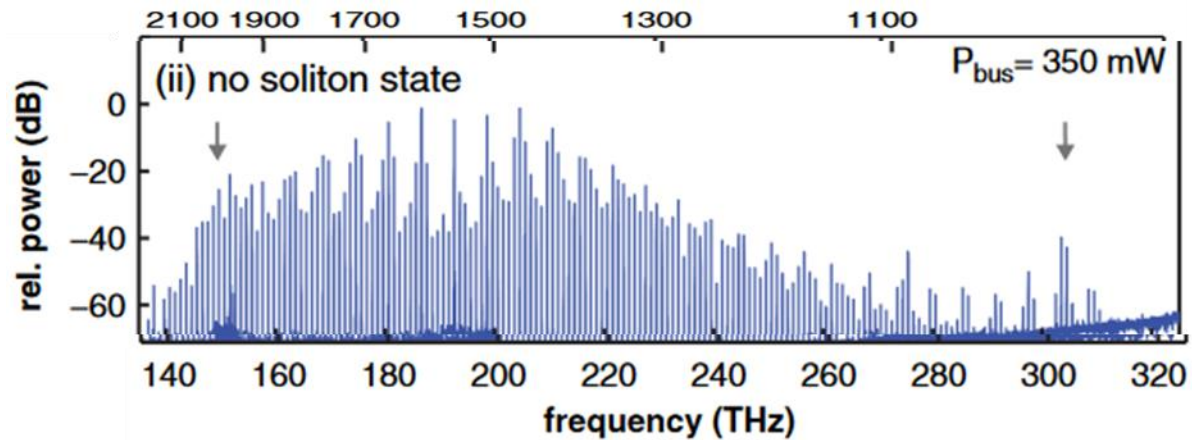
Slow (tens of ns) due to thermal heating
($n = n(T)$)



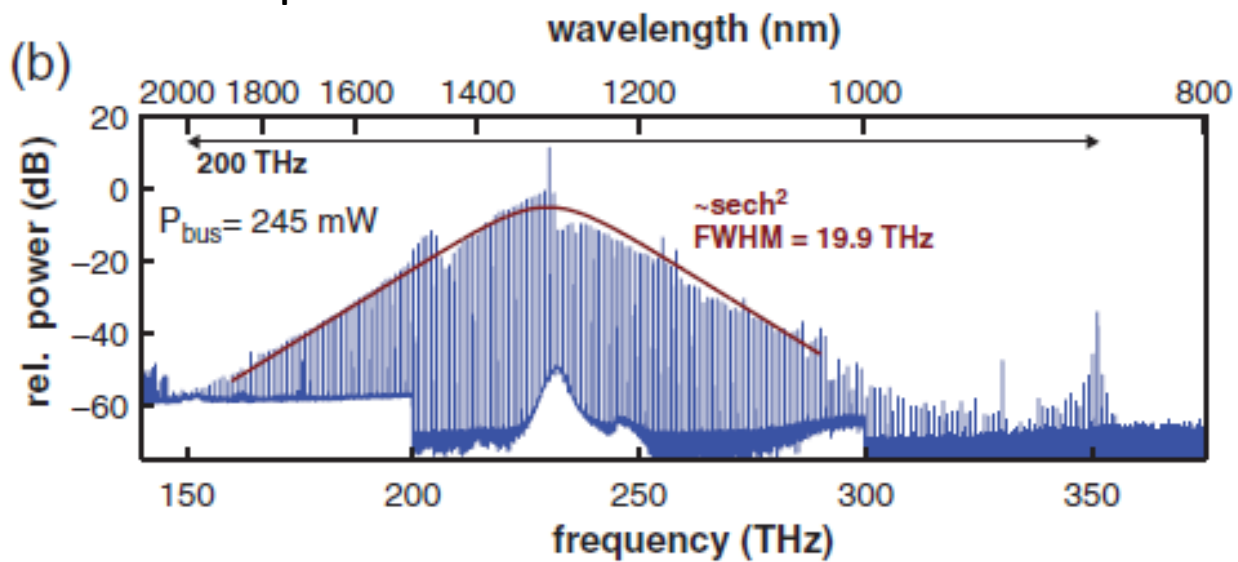
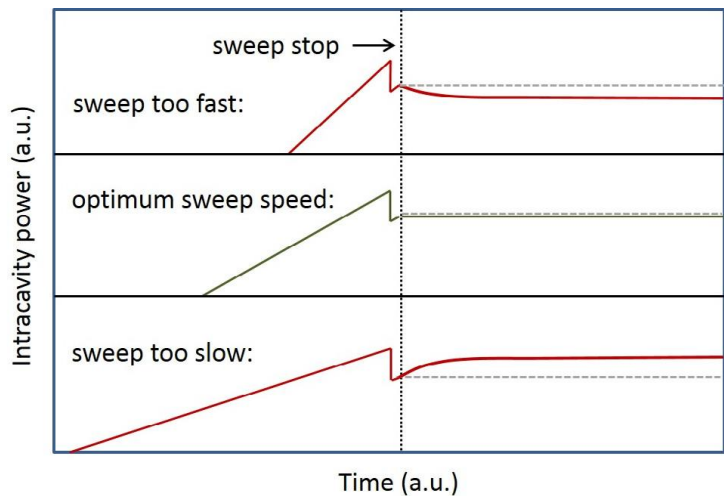
Real life



Chaotic regime



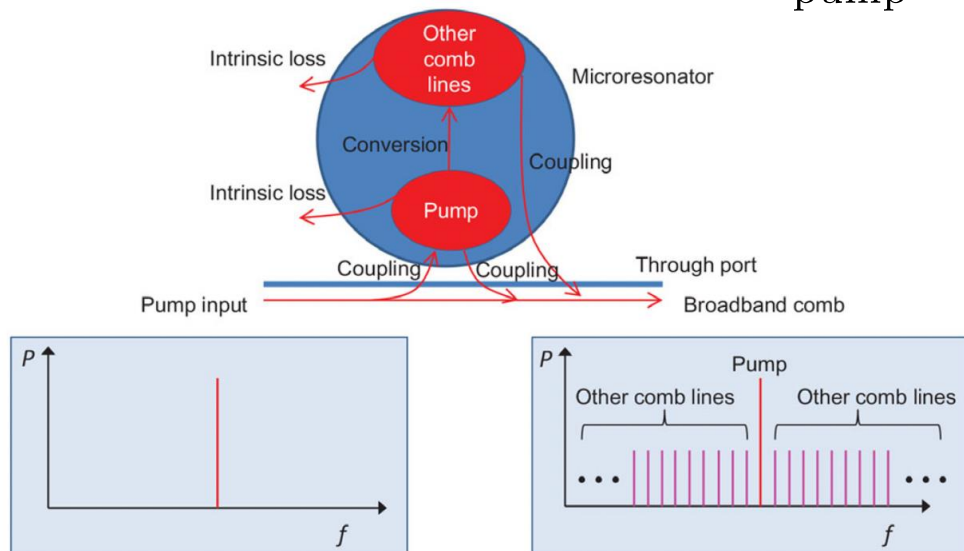
Soliton step



Limitations

- **Low conversion efficiency**

$$\eta = \frac{P_{\text{comb}}^{\text{out}}}{P_{\text{pump}}^{\text{in}}}$$

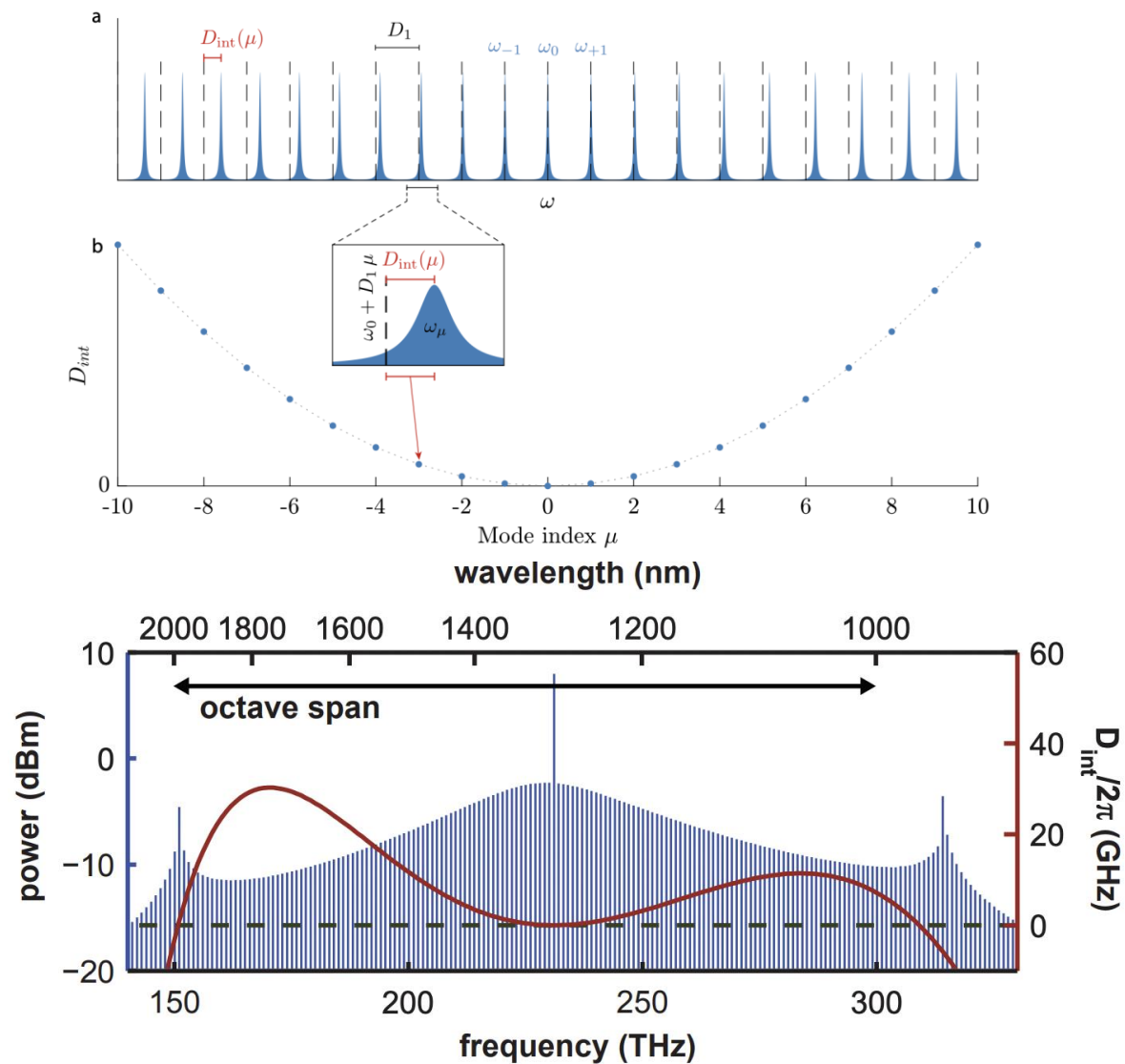


(1 - 4% for single-soliton state microcombs)



Low output power (<<1 mW)

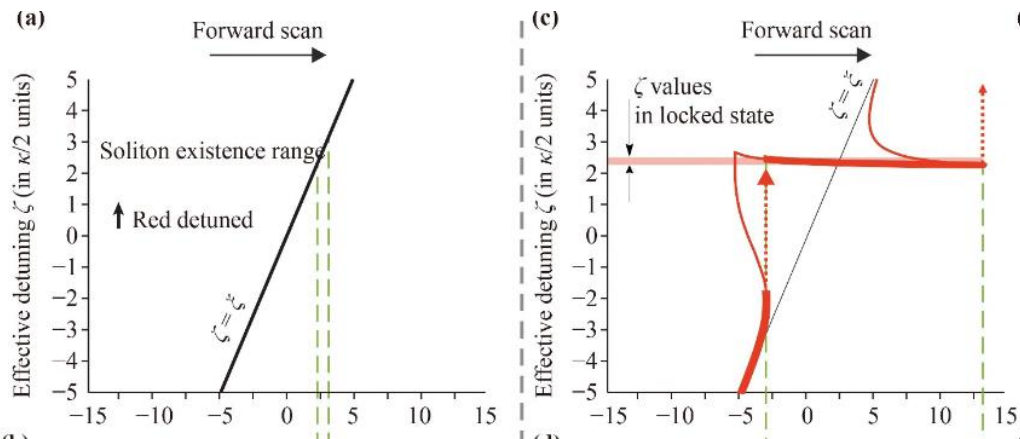
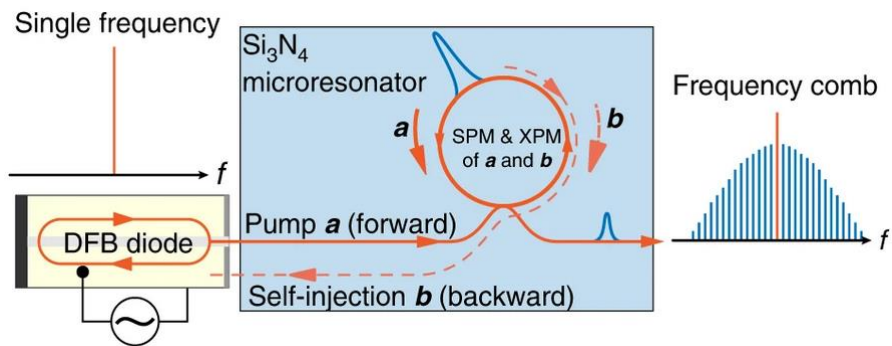
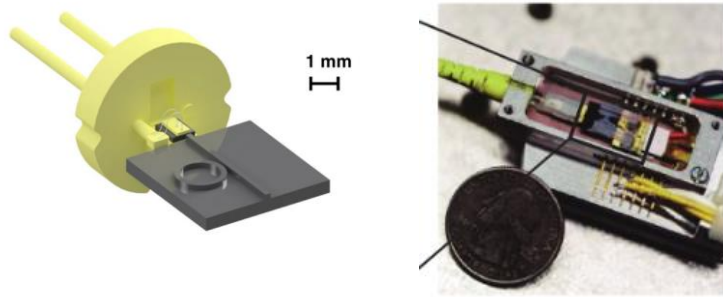
- **Wide combs requires precise dispersion engineering**



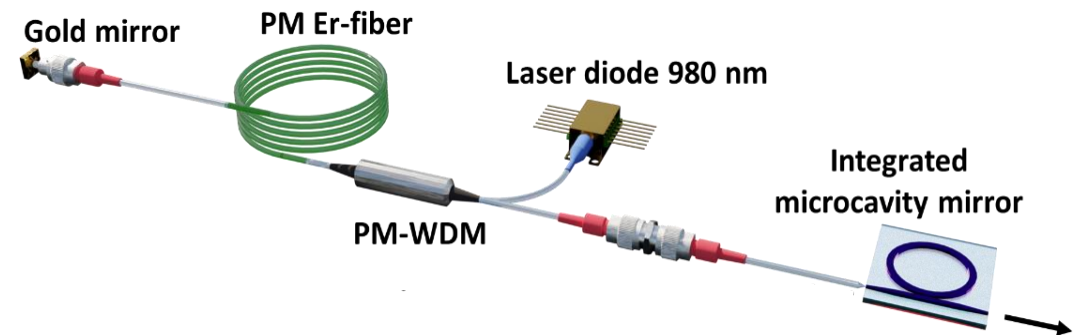
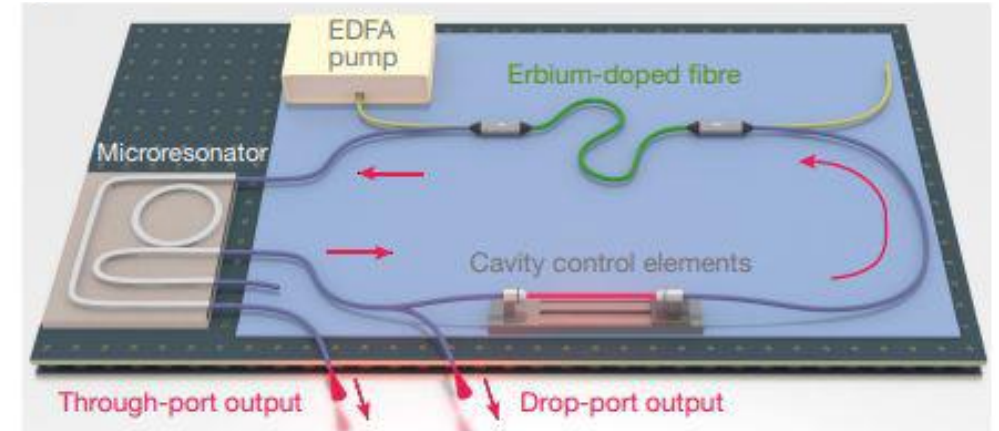
Octave spanning is accessible only for FSR around 1THz

Overcoming limitations

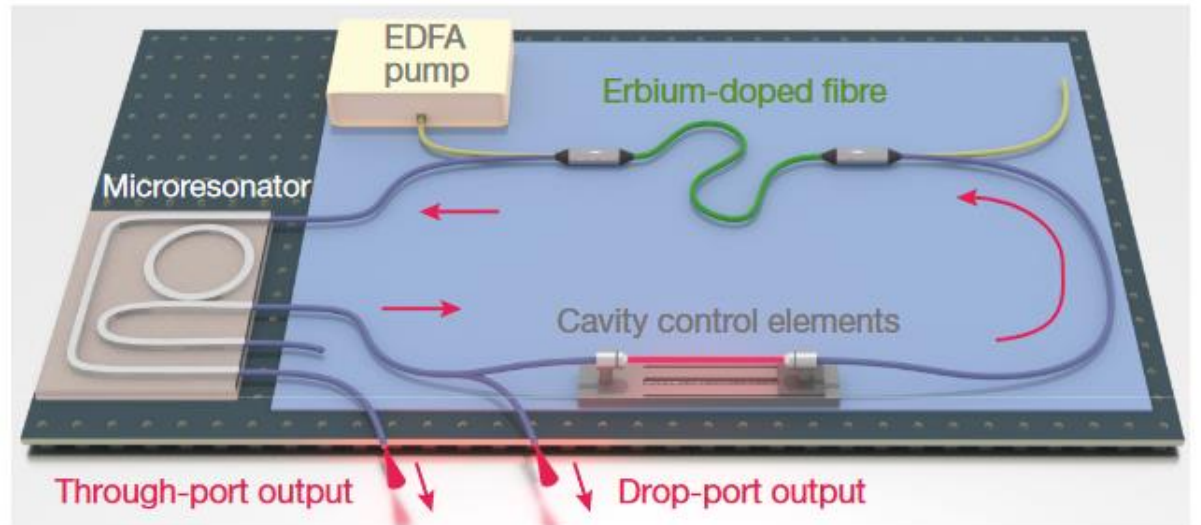
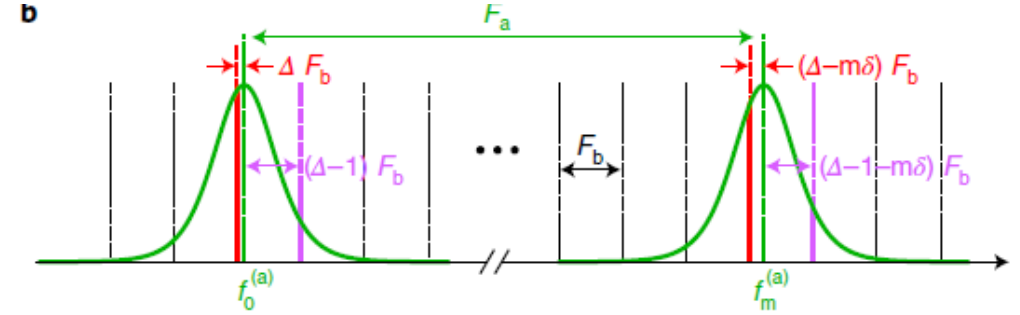
Self-injection locking



Filter driven four wave mixing



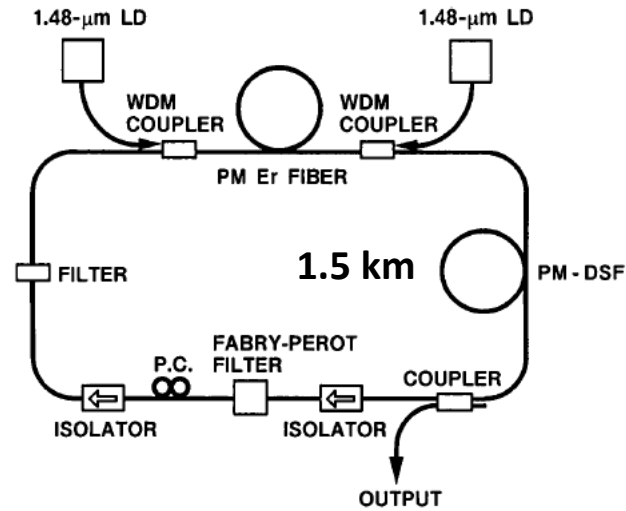
Filter driven four wave mixing



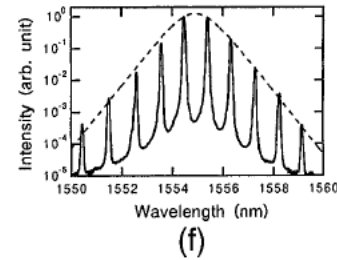
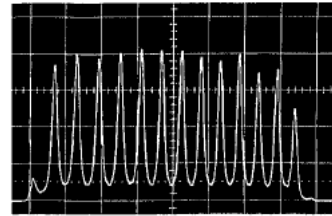
Dissipative four-wave mixing

September 15, 1997 / Vol. 22, No. 18 / OPTICS LETTERS

Eiji Yoshida and Masataka Nakazawa



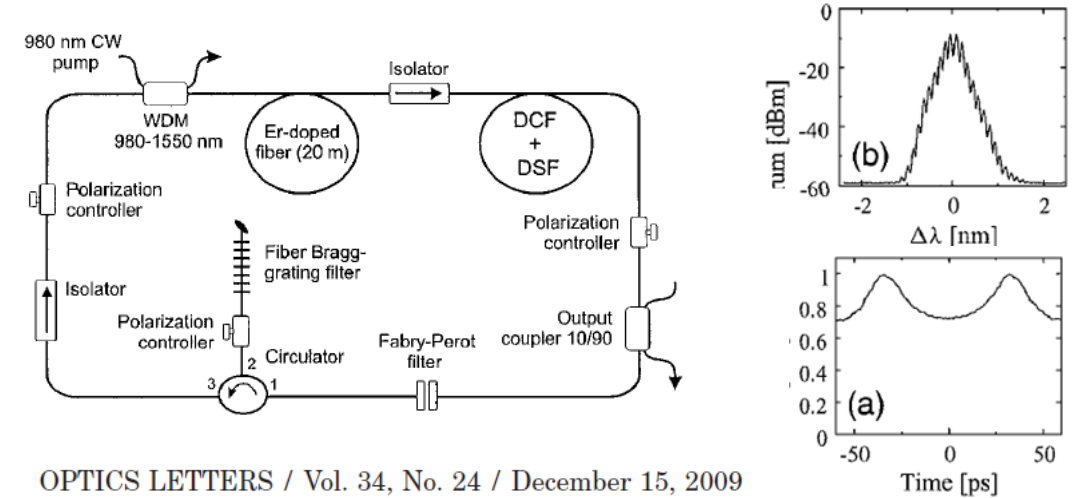
115-GHz pulse train



OPTICS LETTERS / Vol. 27, No. 7 / April 1, 2002

Self-induced modulational instability laser revisited: normal dispersion and dark-pulse train generation

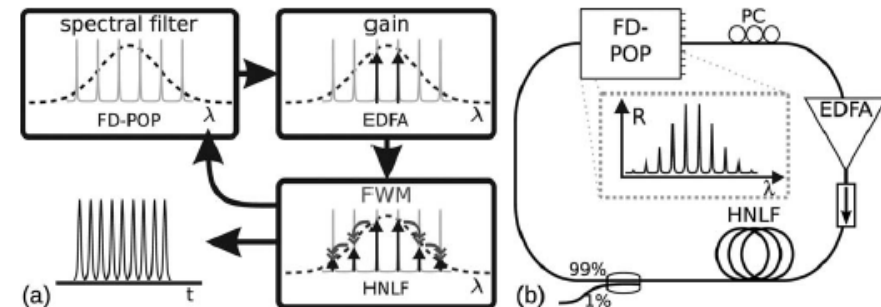
Thibaut Sylvestre,* Stéphane Coen, Philippe Emplit, and Marc Haelterman



OPTICS LETTERS / Vol. 34, No. 24 / December 15, 2009

Repetition-rate-selective, wavelength-tunable mode-locked laser at up to 640 GHz

Jochen Schröder,* Trung D. Vo, and Benjamin J. Eggleton



Vol. 15, No. 4/April 1998/J. Opt. Soc. Am. B

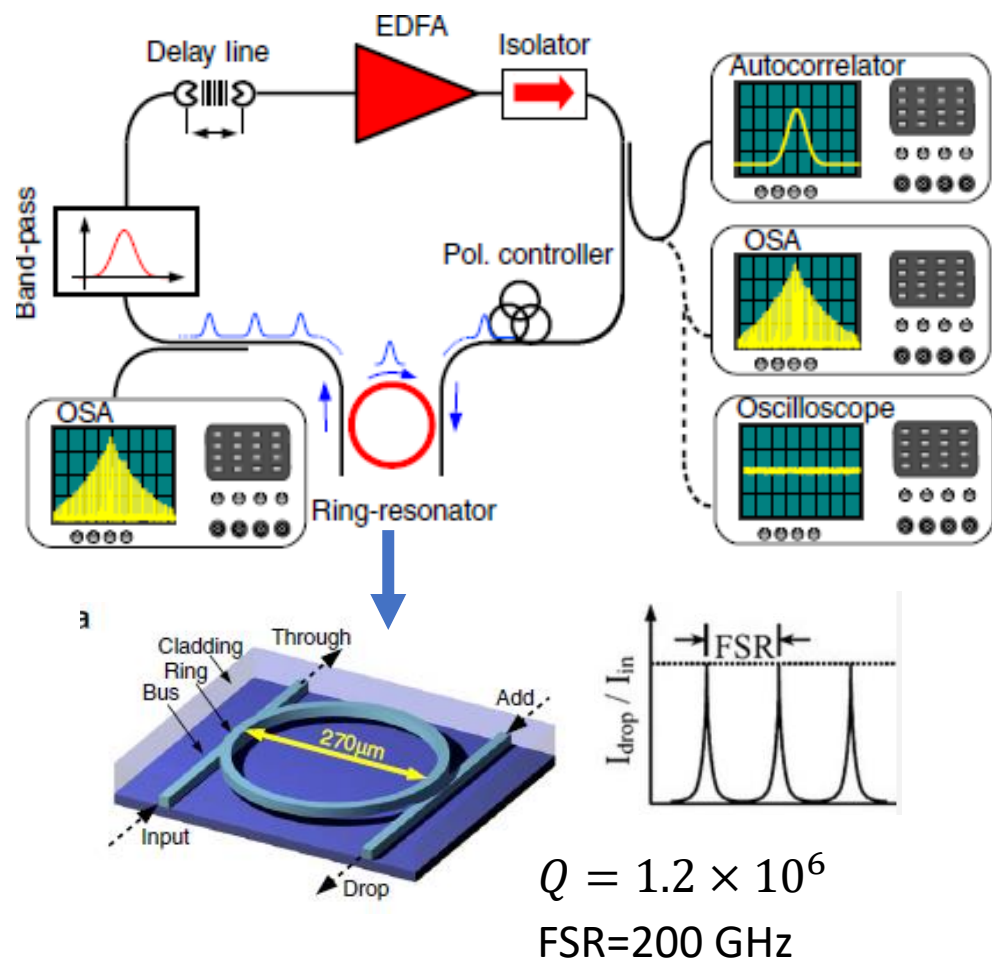
Passive mode locking by dissipative four-wave mixing

M. Quiroga-Teixeiro, C. Balslev Clausen, M. P. So'rgensen, and P. L. Christiansen, P. A. Andrekson

Theoretical description

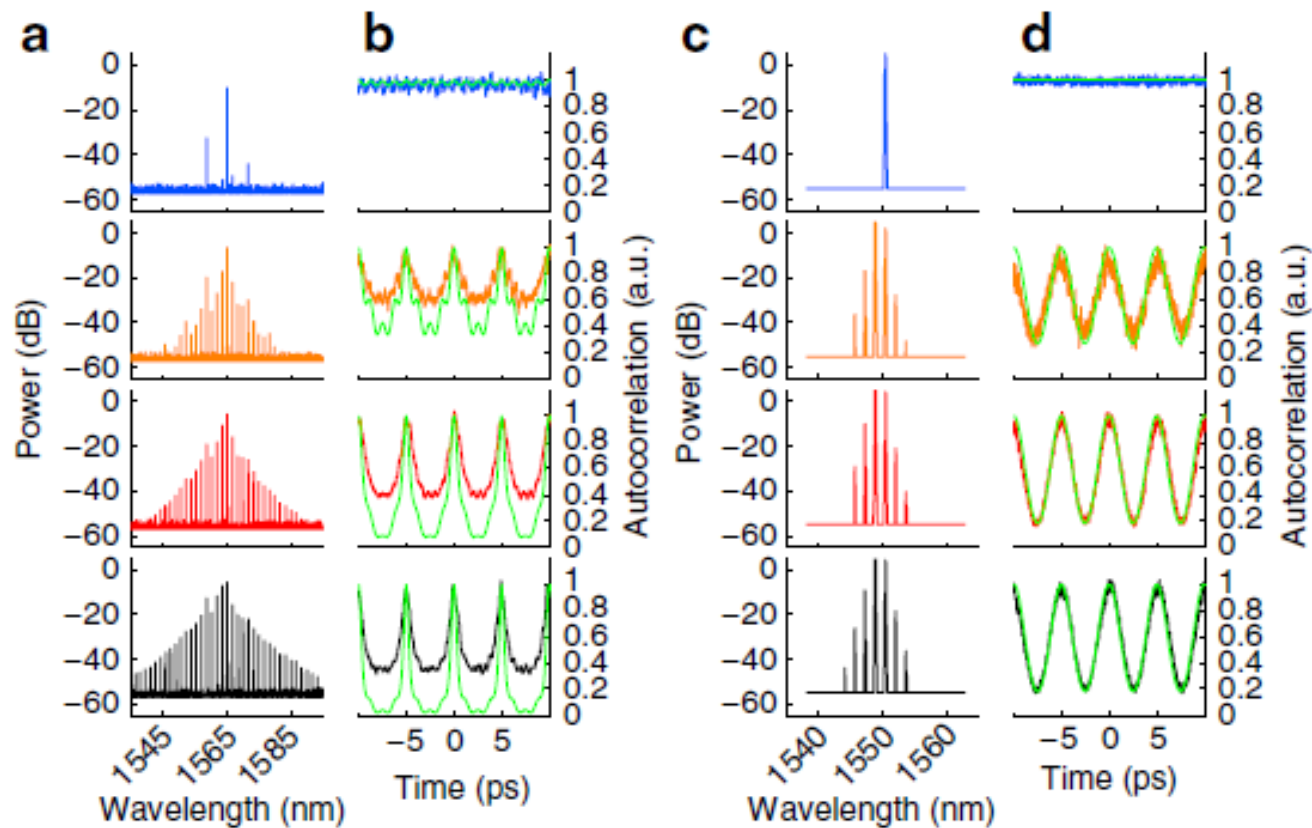
Demonstration of a stable ultrafast laser based on a nonlinear microcavity

M. Peccianti^{1,2}, A. Pasquazi¹, Y. Park¹, B.E. Little³, S.T. Chu^{3,4}, D.J. Moss^{1,5} & R. Morandotti¹



$FSR_{laser} = 6 \text{ MHz}$

$FSR_{laser} = 64 \text{ MHz}$



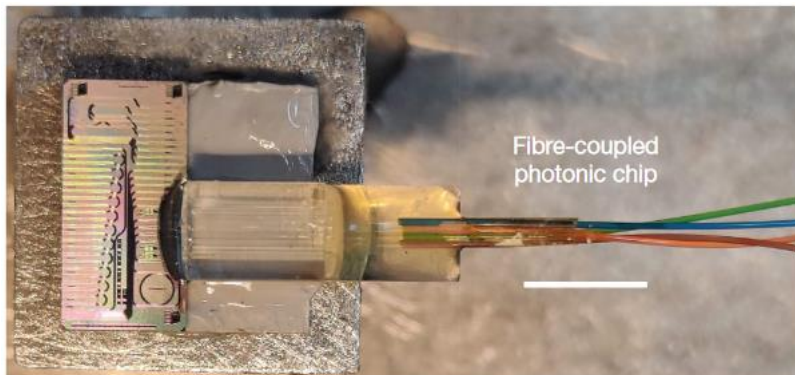
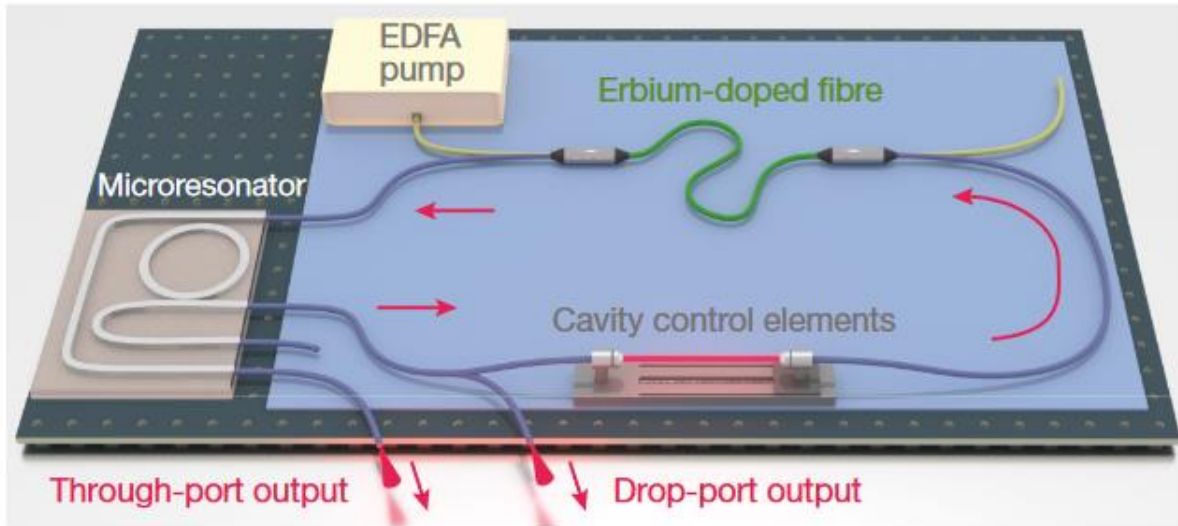
Stable and unstable regimes observed depending on the delay line position

nature

Self-emergence of robust solitons in a microcavity

Nature | Vol 608 | 11 August 2022 | 303

Maxwell Rowley¹, Pierre-Henry Hanzard¹, Antonio Cutrona^{1,2}, Hualong Bao¹, Sai T. Chu³, Brent E. Little⁴, Roberto Morandotti⁵, David J. Moss⁶, Gian-Luca Oppo⁷, Juan Sebastian Toterogongora^{1,2}, Marco Peccianti^{1,2} & Alessia Pasquazi^{1,2}

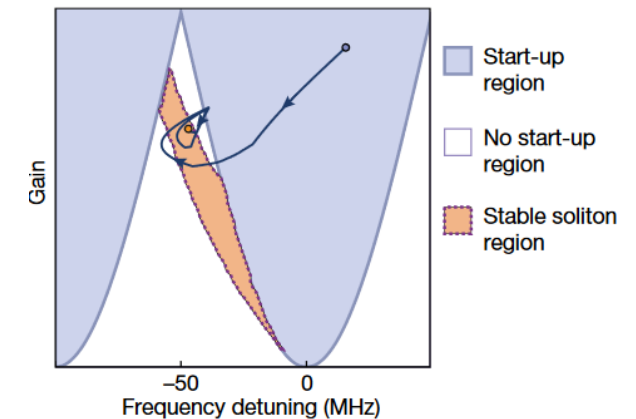
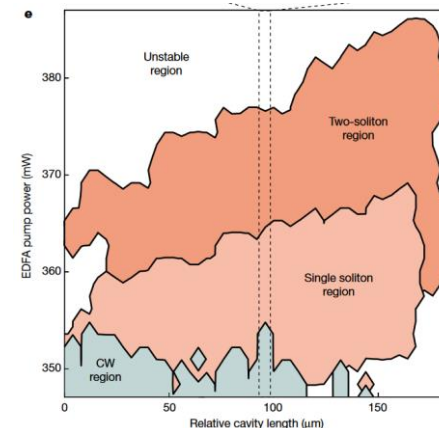
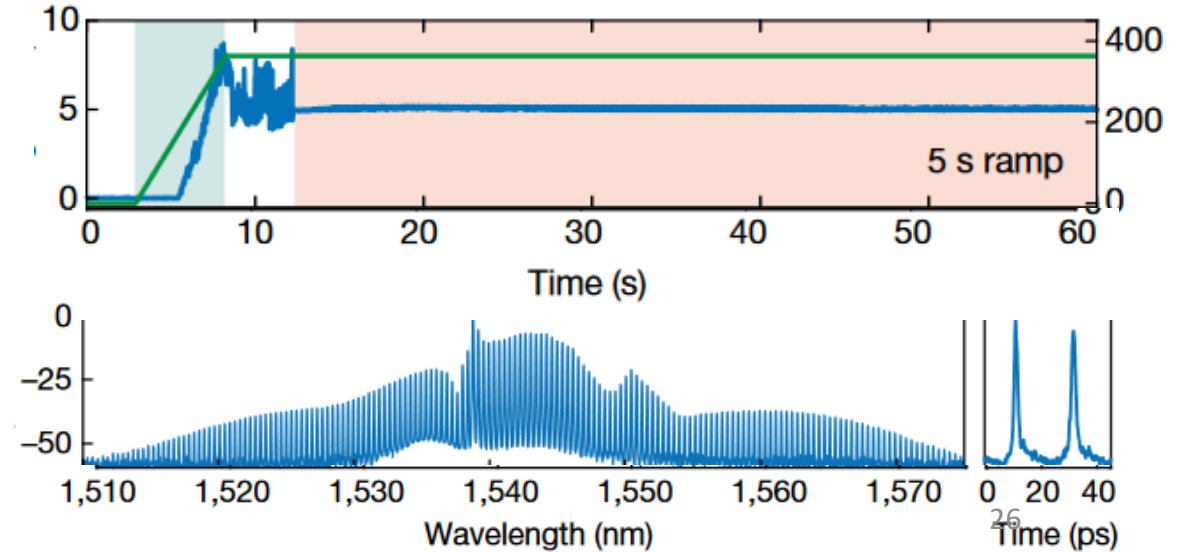


$$FSR_{cavity} = 49.8 \text{ GHz}$$

$$\text{Linewidth} = 120 \text{ MHz}$$

$$FSR_{laser} = 95 \text{ MHz}$$

Main claim: Fine tuning of laser cavity parameters makes soliton a main attractor

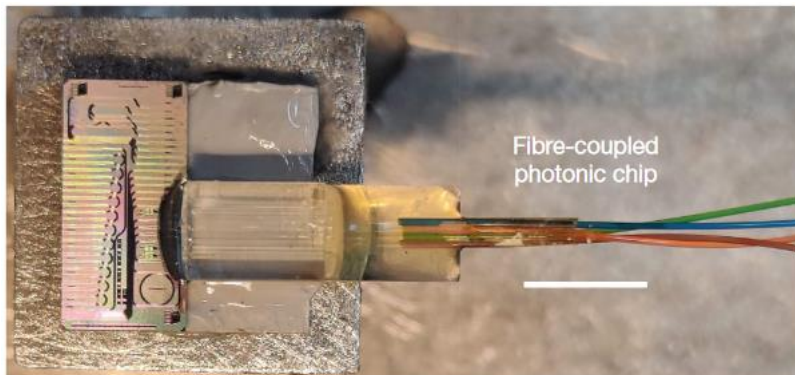
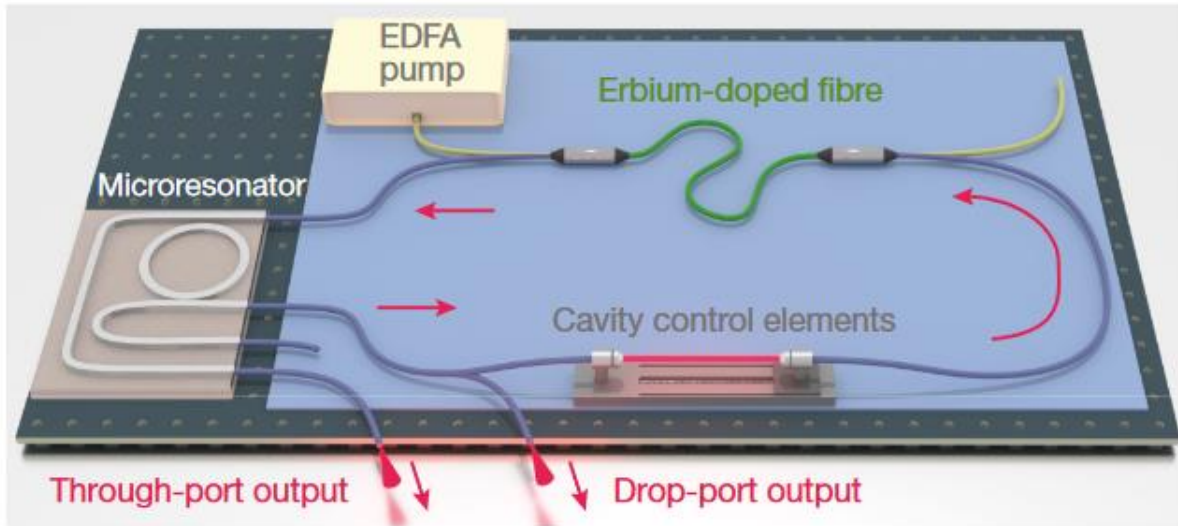


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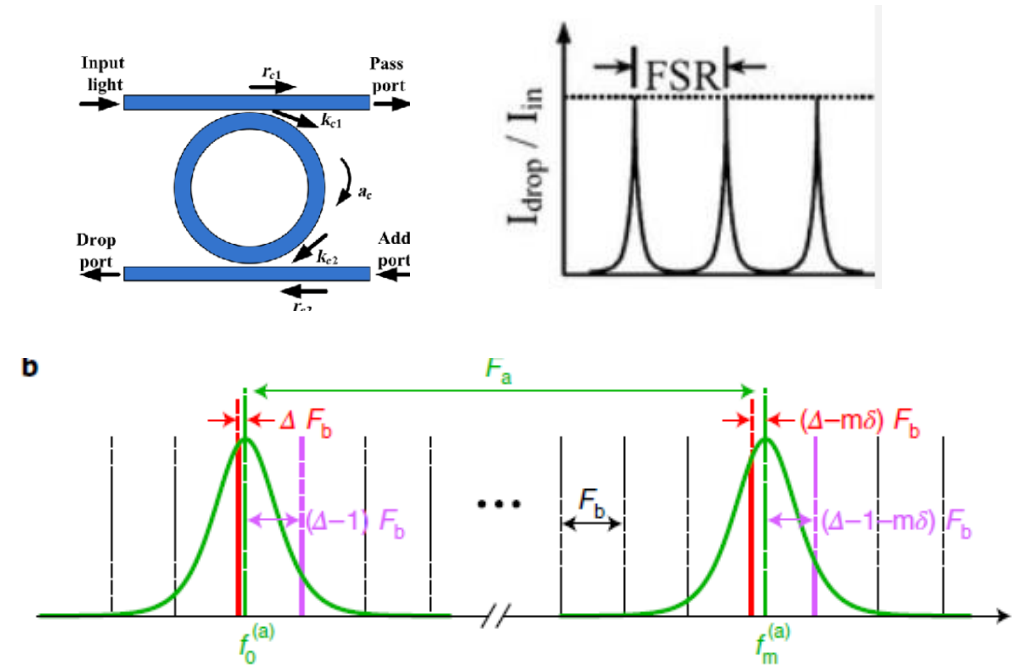


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Microring has two roles:

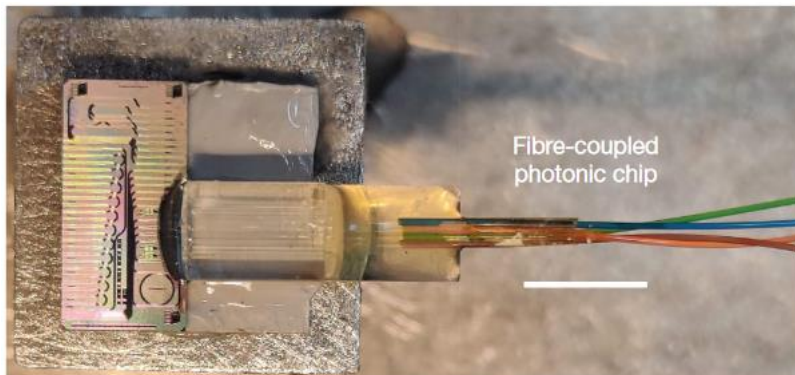
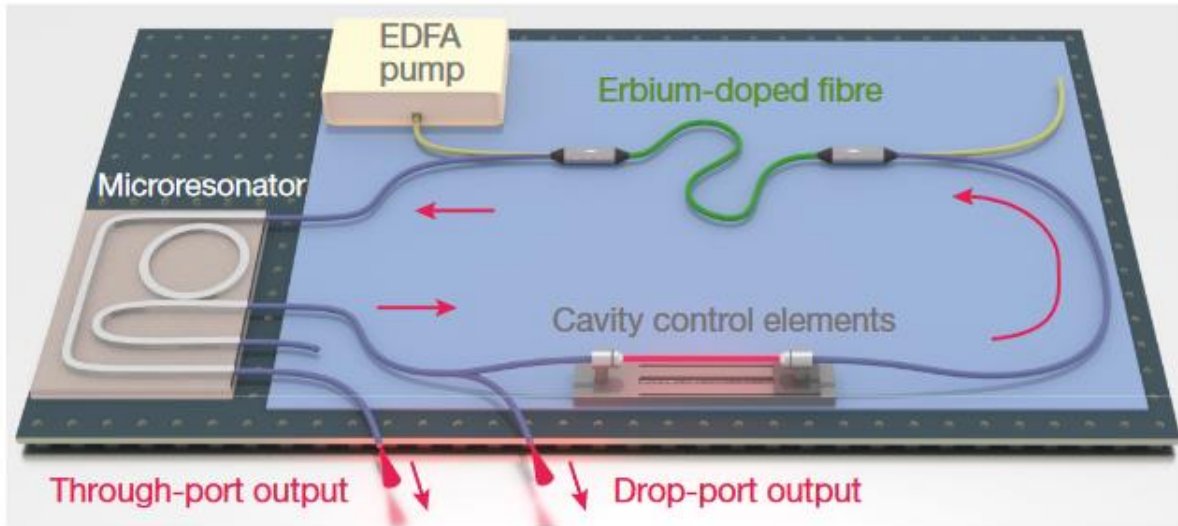
- Increase spectra by four wave mixing
- Filter laser modes to leave only every N^{th} mode

nature

Self-emergence of robust solitons in a microcavity

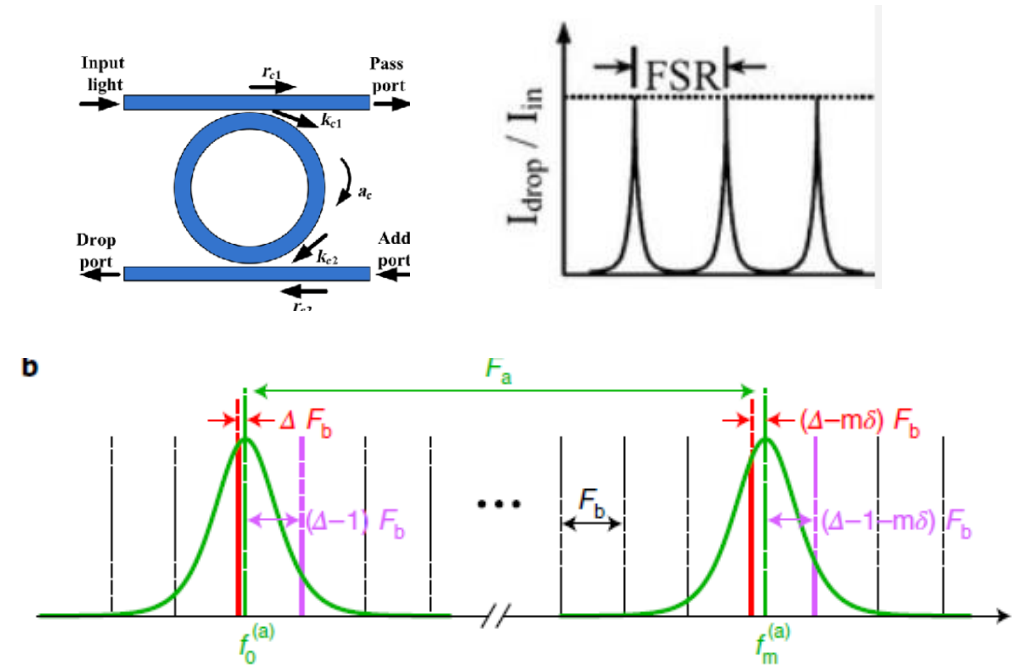
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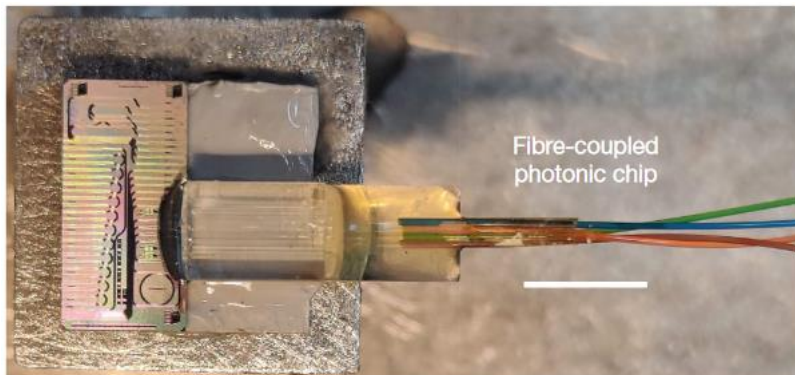
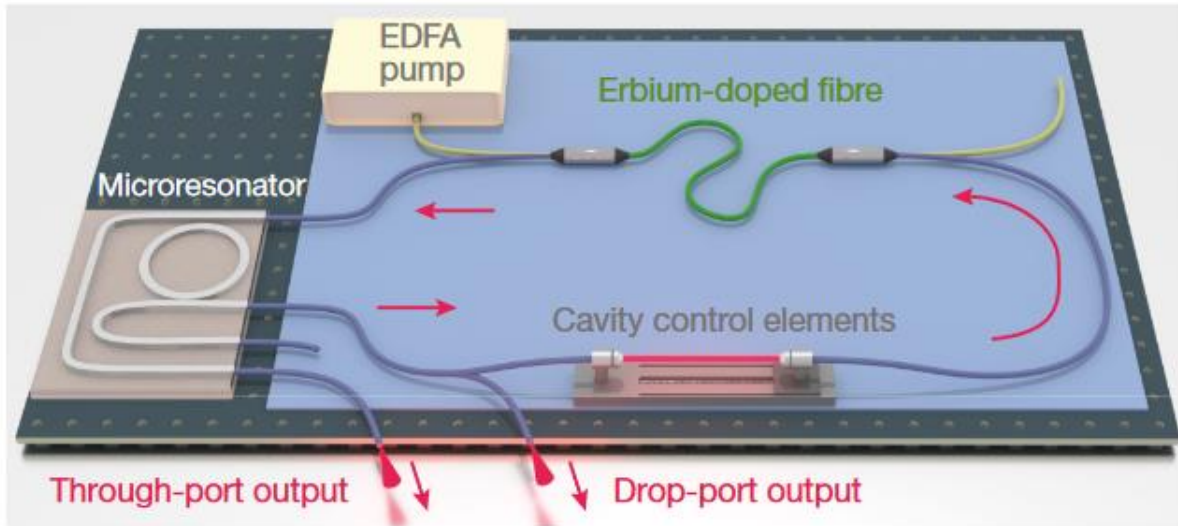
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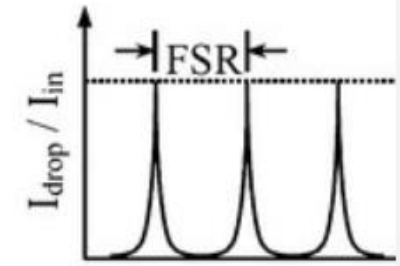
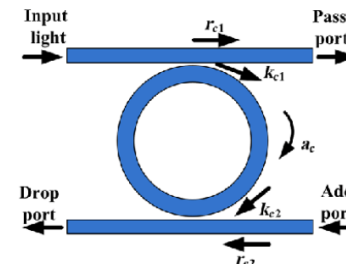


$$FSR_{cavity} = 49.8 \text{ GHz}$$

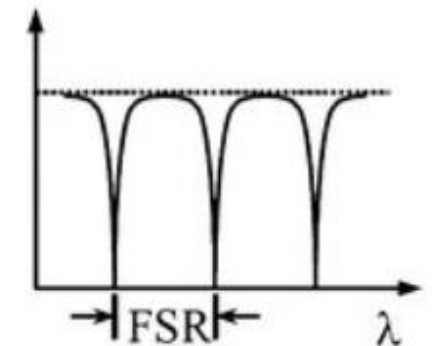
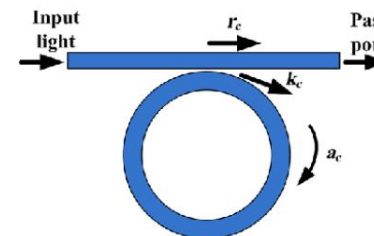
$$\text{Linewidth} = 120 \text{ MHz}$$

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Main claim: Fine tuning of laser cavity parameters makes soliton a main attractor

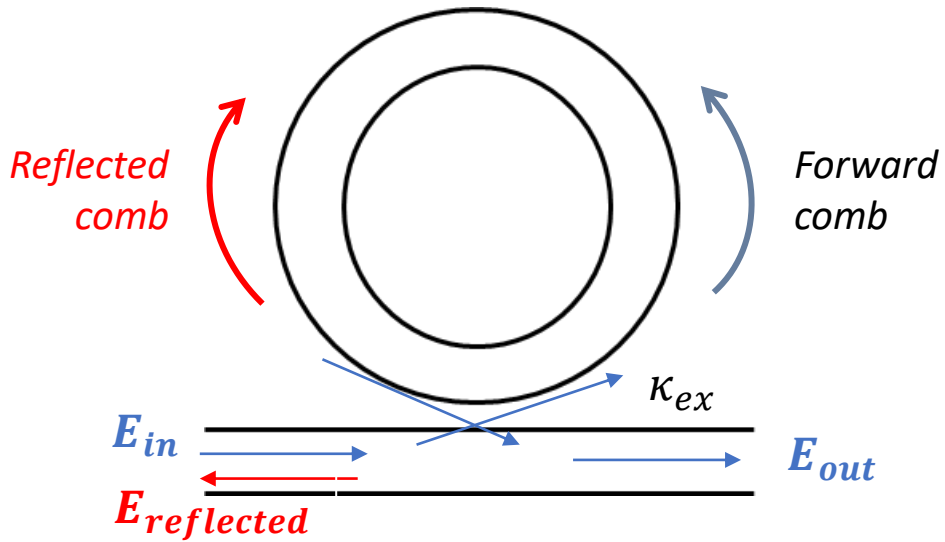


Is it possible to use 2-port microcavity?



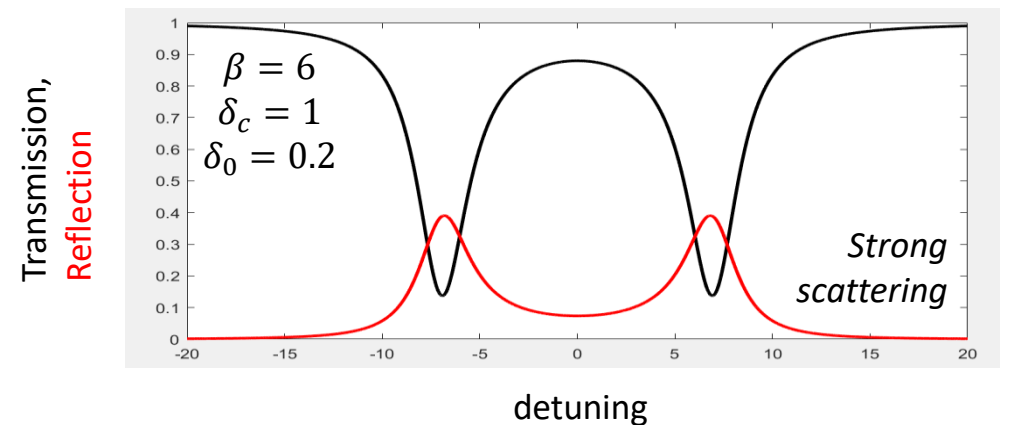
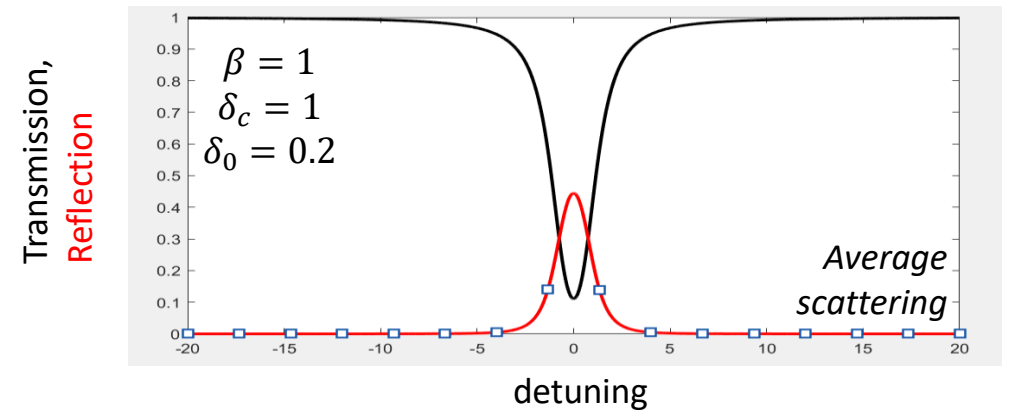
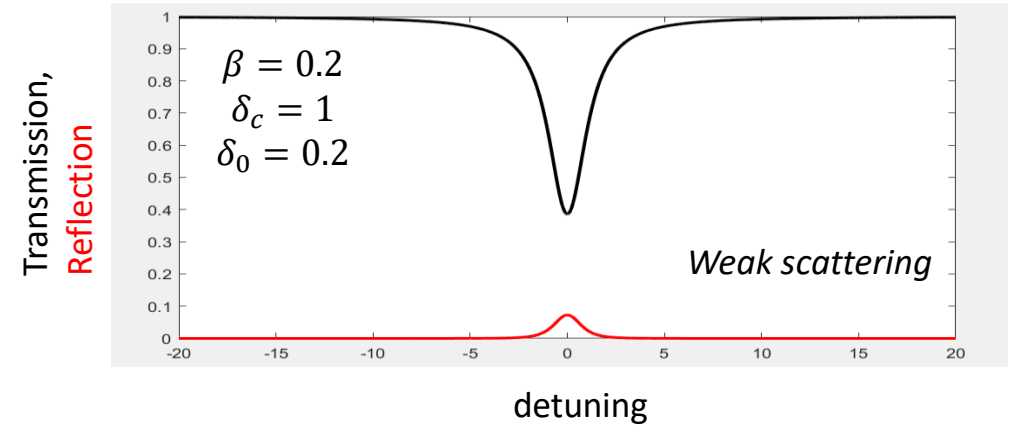
Spontaneous creation of reflected comb

One more player - **Rayleigh scattering**

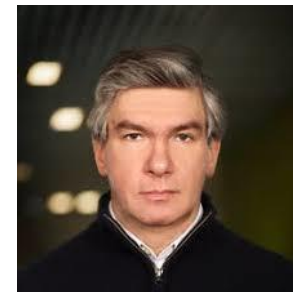


In high-Q microcavity **Rayleigh scattering** is enhanced by factor, similar to **Purcell factor** -> spontaneous back reflected comb formation.

β – Rayleigh scattering
 δ_c – coupling losses
 δ_0 – cavity losses

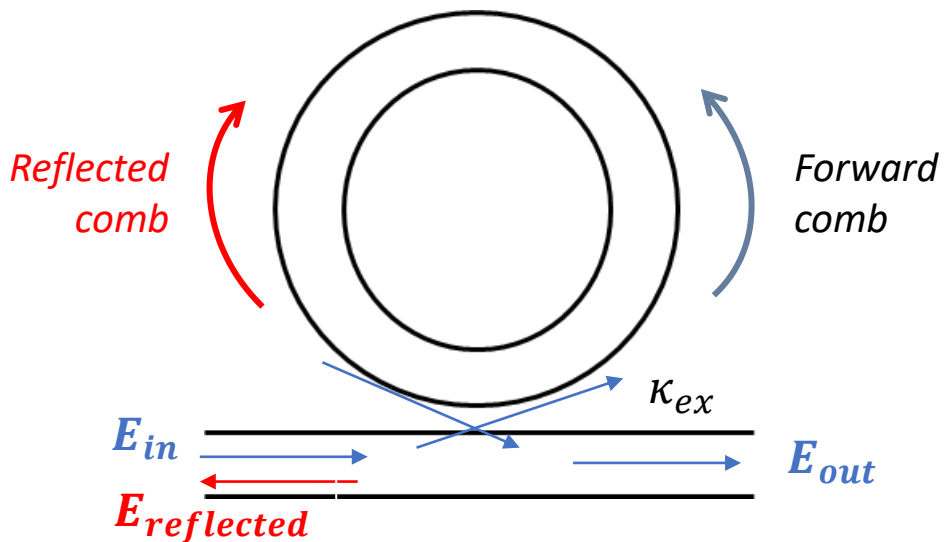


Spontaneous creation of reflected comb

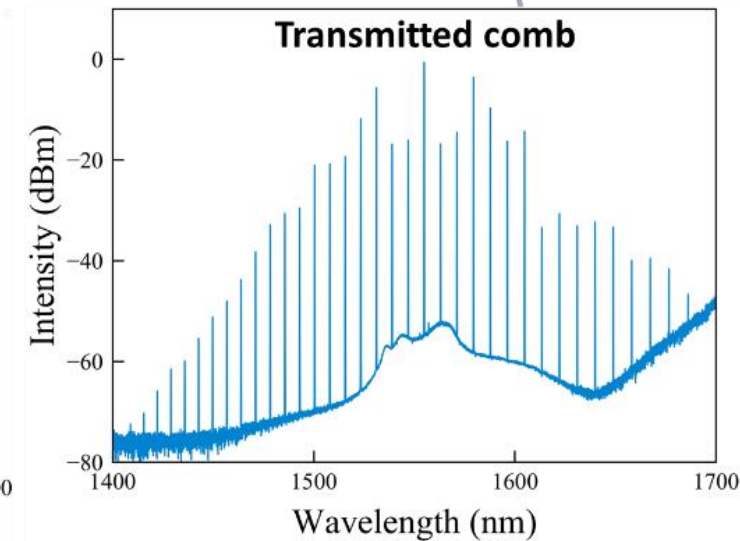
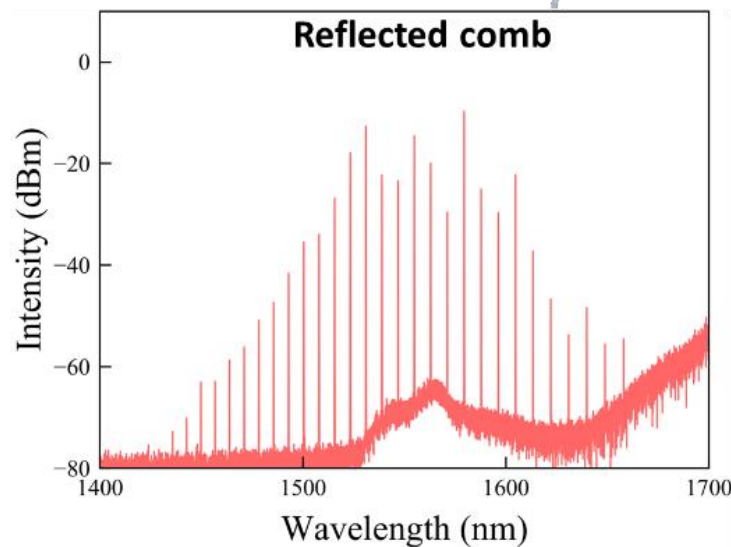
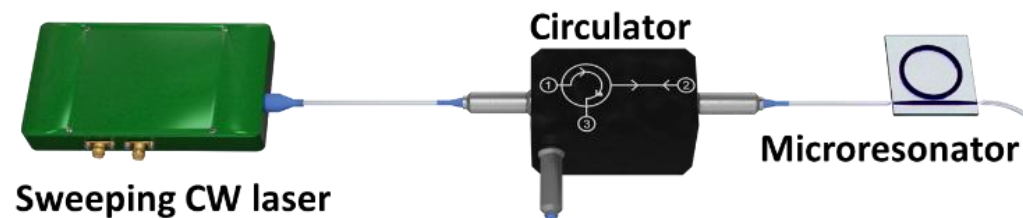


Igor Bilenko

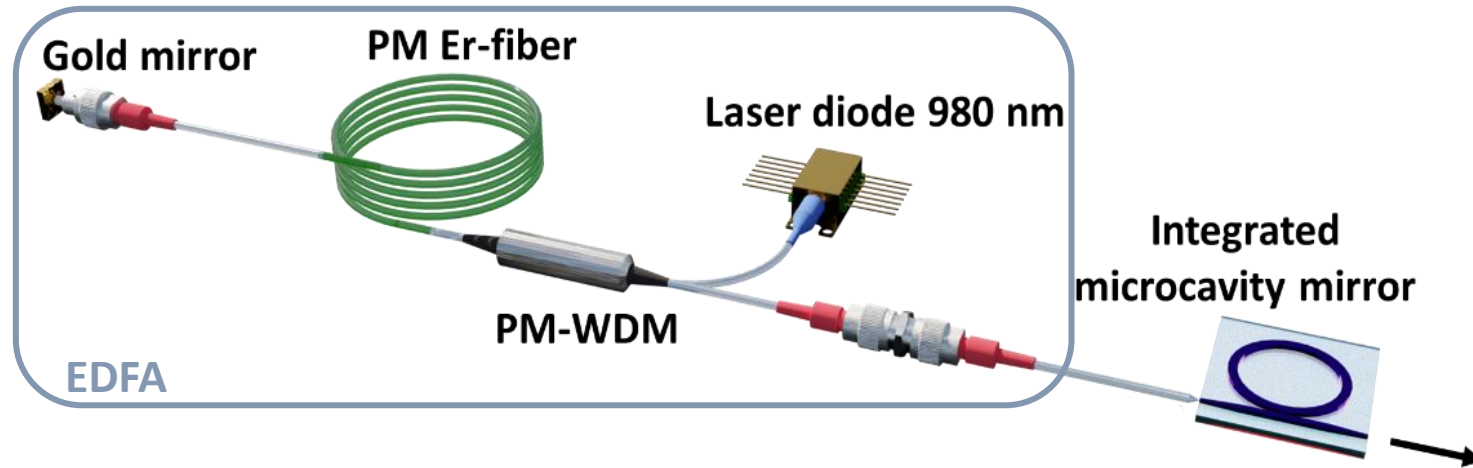
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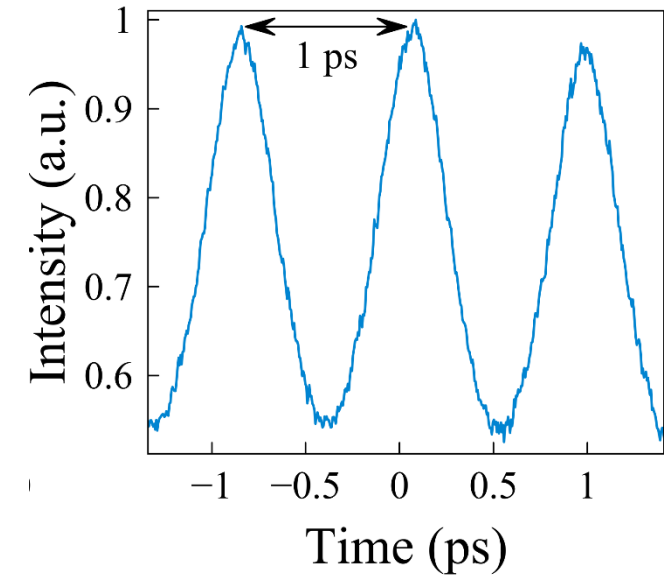
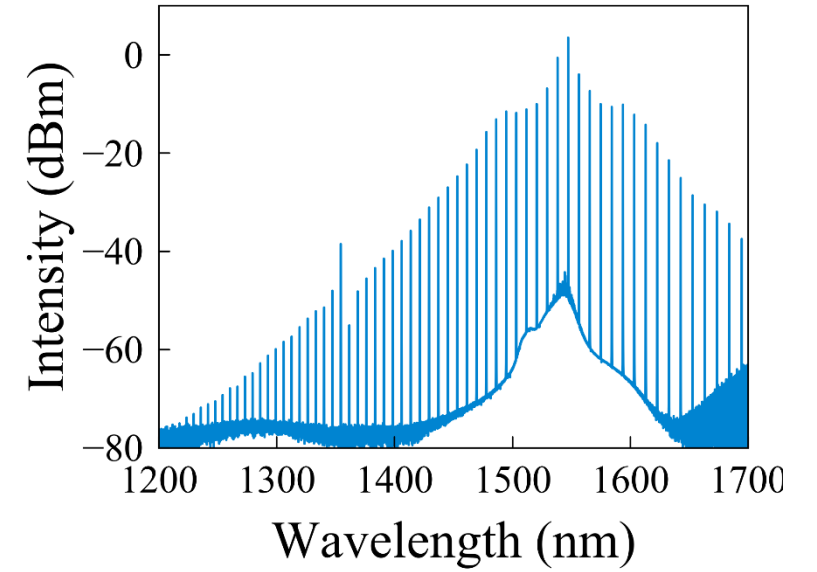
Microcavity as a semi-reflective mirror



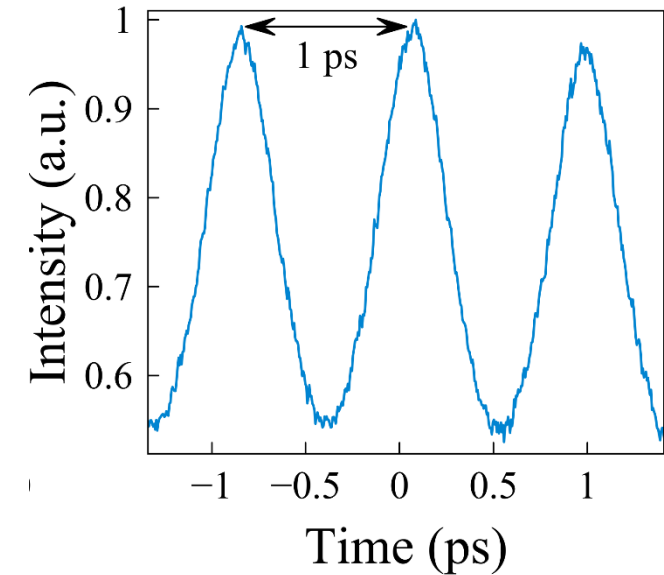
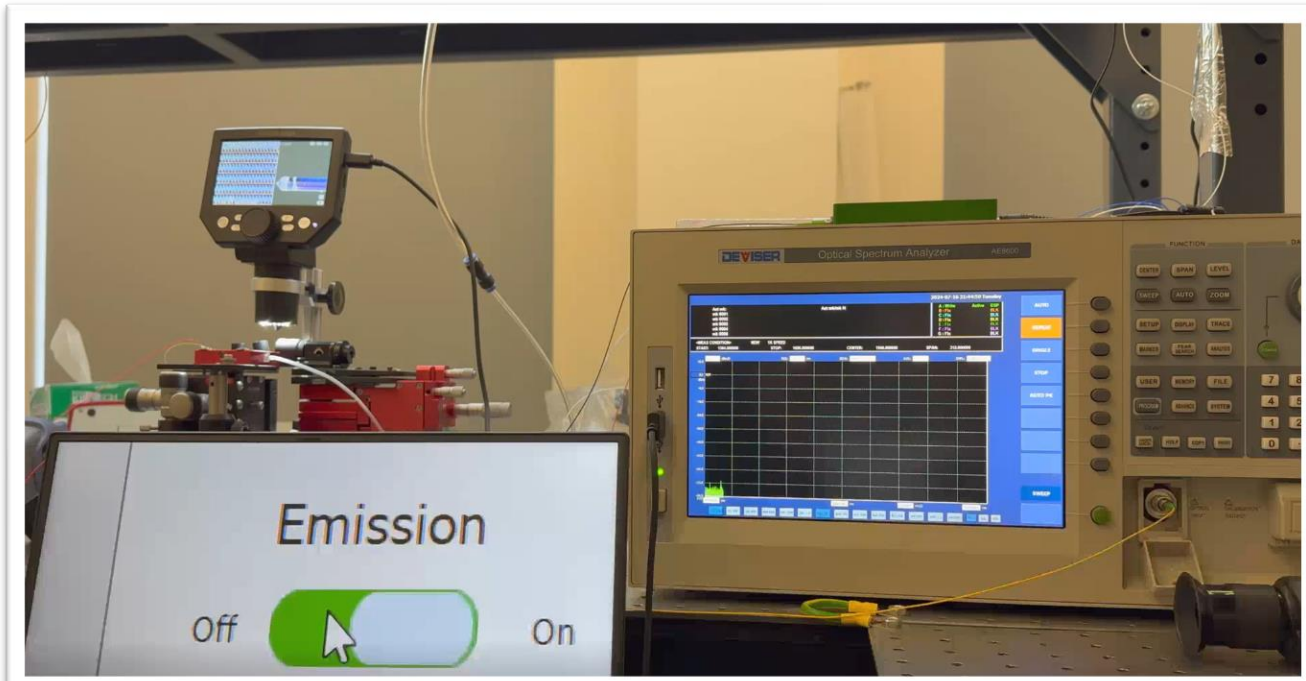
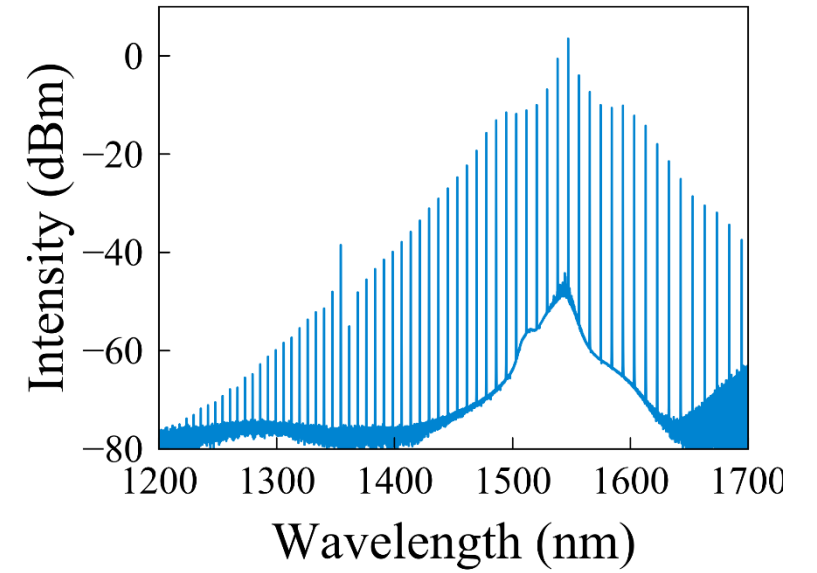
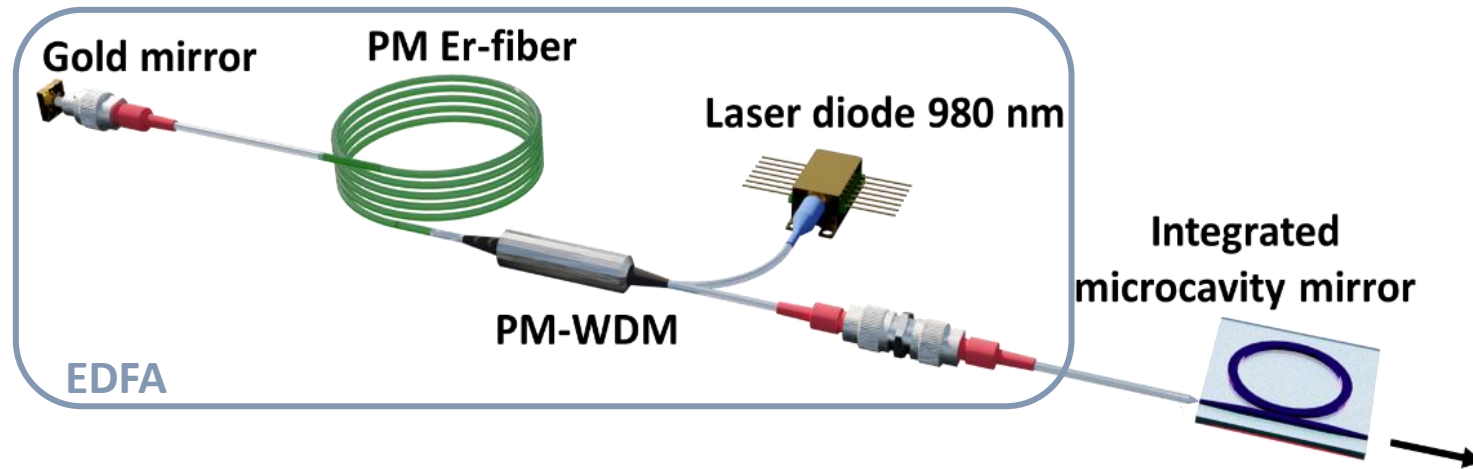
$$FSR_{laser} = 35 \text{ MHz}$$

$$FSR_{cavity} = 1 \text{ THz}$$

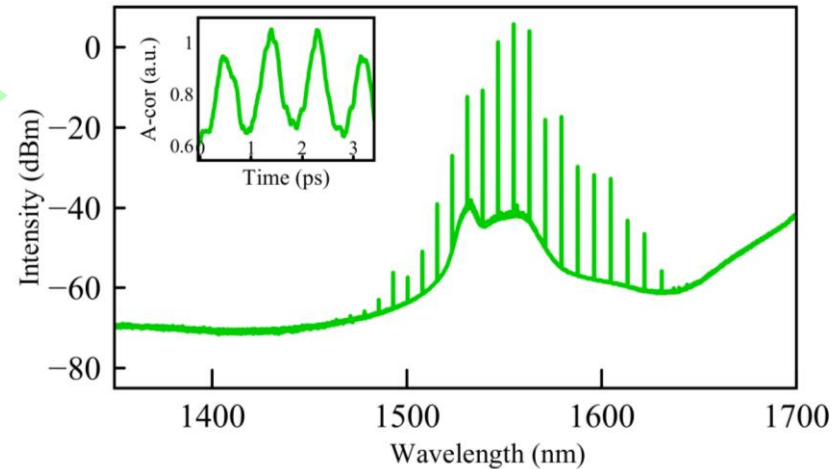
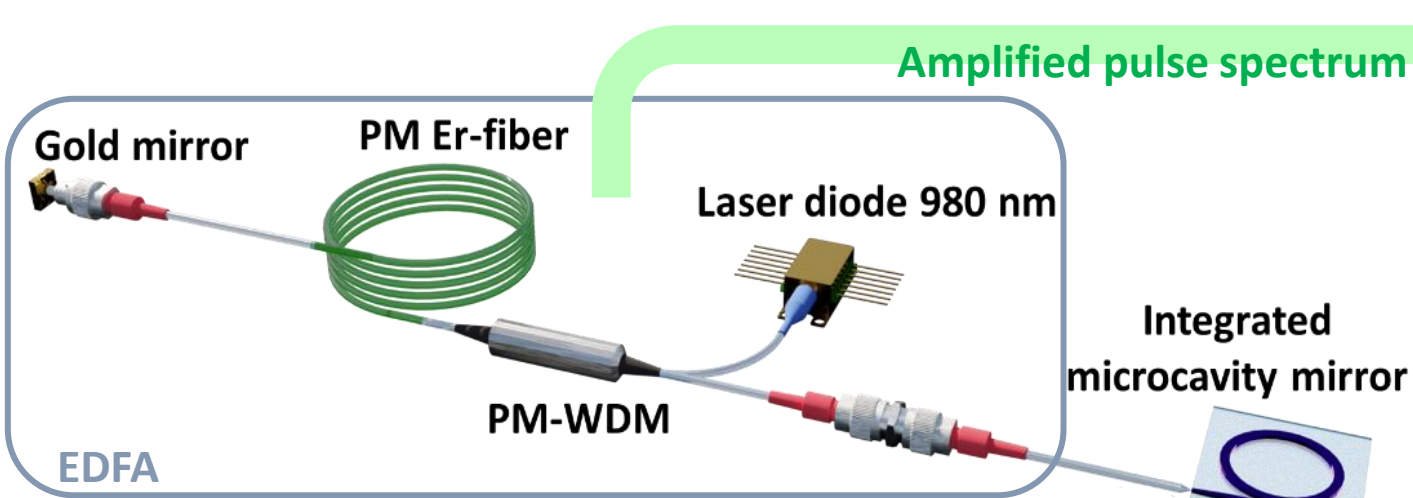
$$Linewidth = 150 \text{ MHz}$$



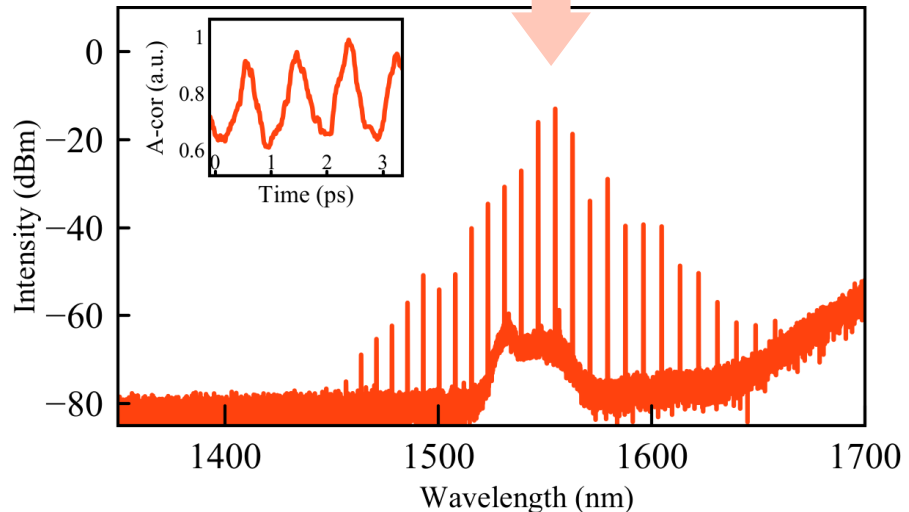
Microcavity as a semi-reflective mirror



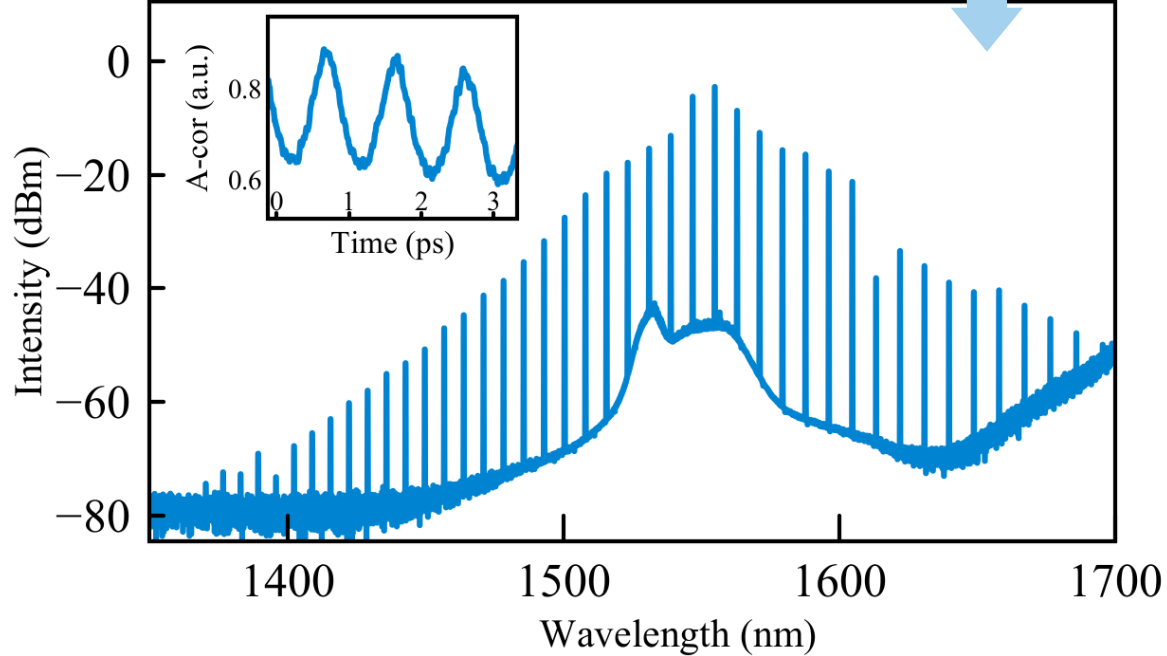
Microcavity as a semi-reflective mirror



Reflected pulse spectrum



Output pulse spectrum



back reflection from the ring due to Rayleigh scattering creates a feedback system

Acknowledgements



Skoltech

Skolkovo Institute of Science and Technology

Skoltech

Dr. Aram Mkrtchyan
Mikhail Mishevskiy
Zohran Ali
Anastasia Netrusova
Prof. Albert Nasibulin



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Igor Bilenko
Nikita Dmitriev
Dmitry Chermoschentcev
Kirill Minkov



Fiber optic research center

Mikhail Melkumov
Sergei Firstov
Alexander Vakhrushev

Thank you for
your attention!